

Vorlesungen Mechatronik im Wintersemester

Vibrations in Nuclear Applications

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TECHNISCHE
UNIVERSITÄT
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Pump Vibration Problems in Power Plants

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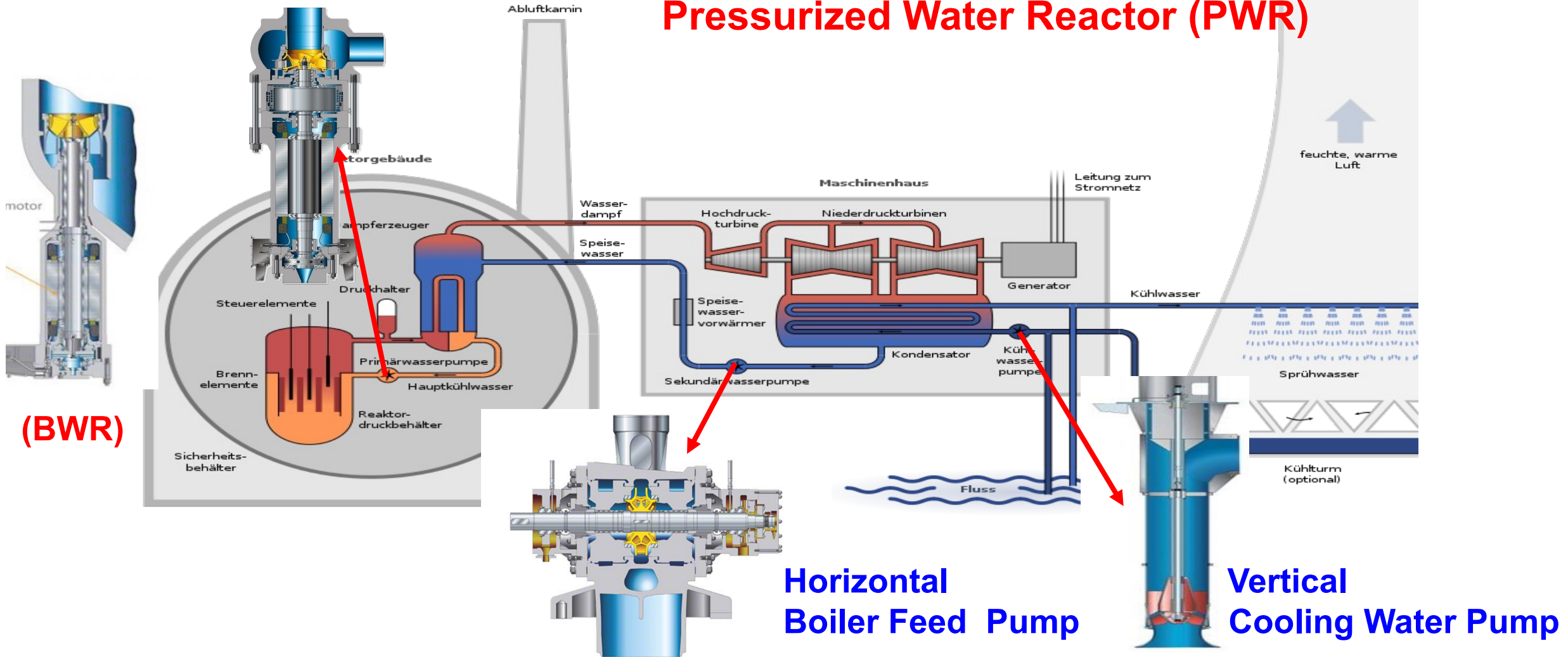
Pump Vibrations in Power Plants

- **Different Vertical and Horizontal Pumps in Power Plants**
- **A typical Vertical Pump System for a Nuclear Power Plant**
- **Vibration Phenomena in Pump Systems**
- **Modeling of Pump Systems to predict Vibration Phenomena**
- **Monitoring of Pump Systems for Vibration Control**
- **Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces**
- **Vibrations of Vertical Pumps due to Unbalance and Instability**

Different Vertical and Horizontal Pumps in Nuclear Power Plants

Vertical Reactor Coolant Pumps (PWR)

Nuclear Power Plant Pressurized Water Reactor (PWR)



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A typical Vertical Pump System for a Nuclear Power Plant



Source: KSB Handbook

Vertical Reactor Coolant Pump

with

Impeller and Guide Vane

Flywheel

Electric Motor Drive

Three Radial Fluid Bearings

Axial Fluid Bearing

Pump Casing

A typical Vertical Pump System for a Nuclear Power Plant



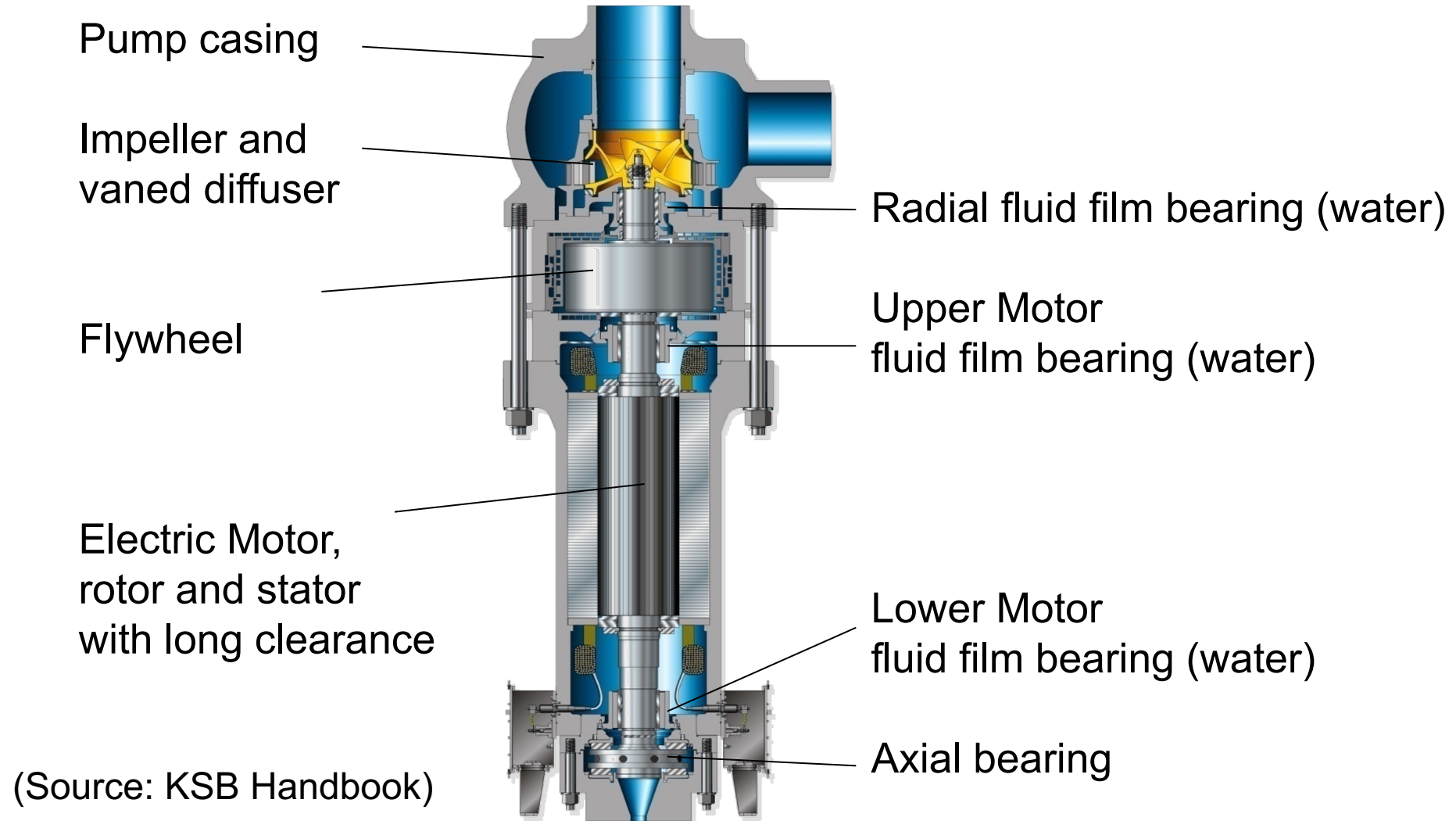
Source: KSB Handbook

Vertical Reactor Coolant Pump

Pump Characteristics

Power	kW
Capacity	m ³ /h
Head	m
Pressure	bar
Temperature	°C
Rotational Speeds	rpm

A typical Vertical Pump System for a Nuclear Power Plant

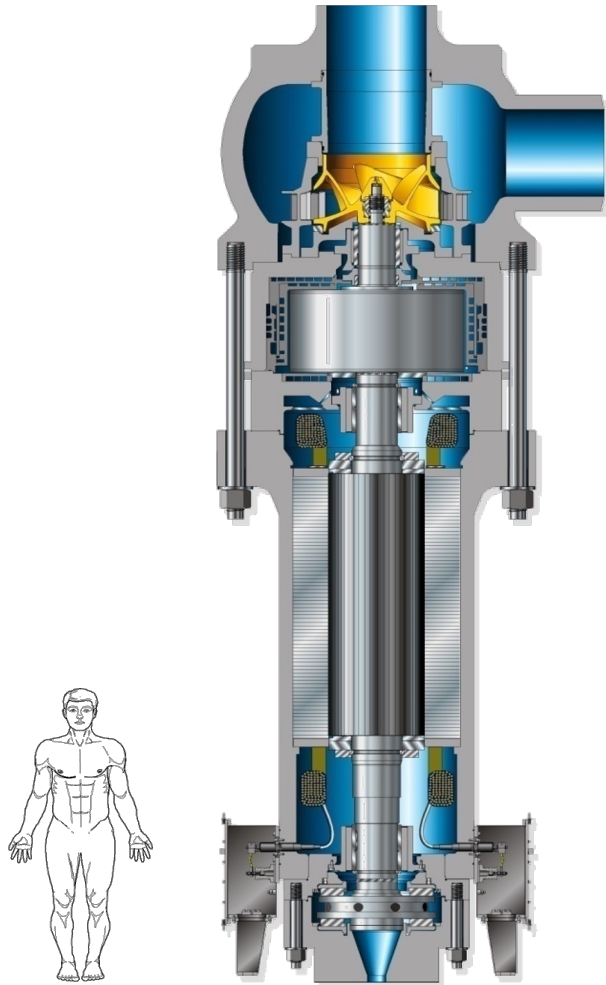


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Vibration Phenomena in Pump Systems

Overview



Vibrations of Vertical Pumps
Fluid Dynamics & Mechanics

Stresses
Material Strengths

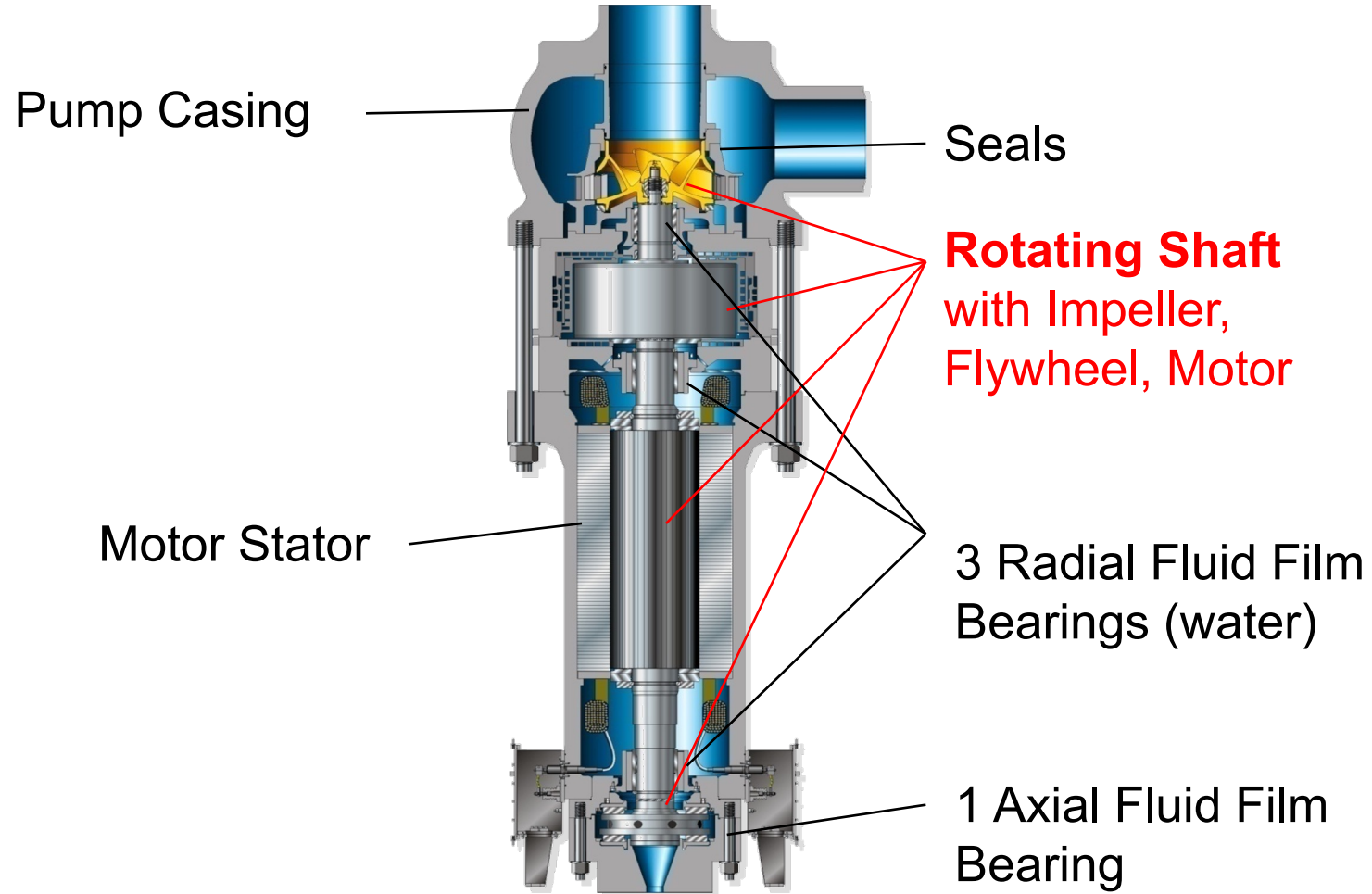
Rotordynamics with
Interaction Effects

Unbalance Vibrations,
Critical Speeds,
Vibrations due to
Rotor Fluid Interactions and
Rotor Structure Interactions

Rotor
Instability,
Whirl and
Whip

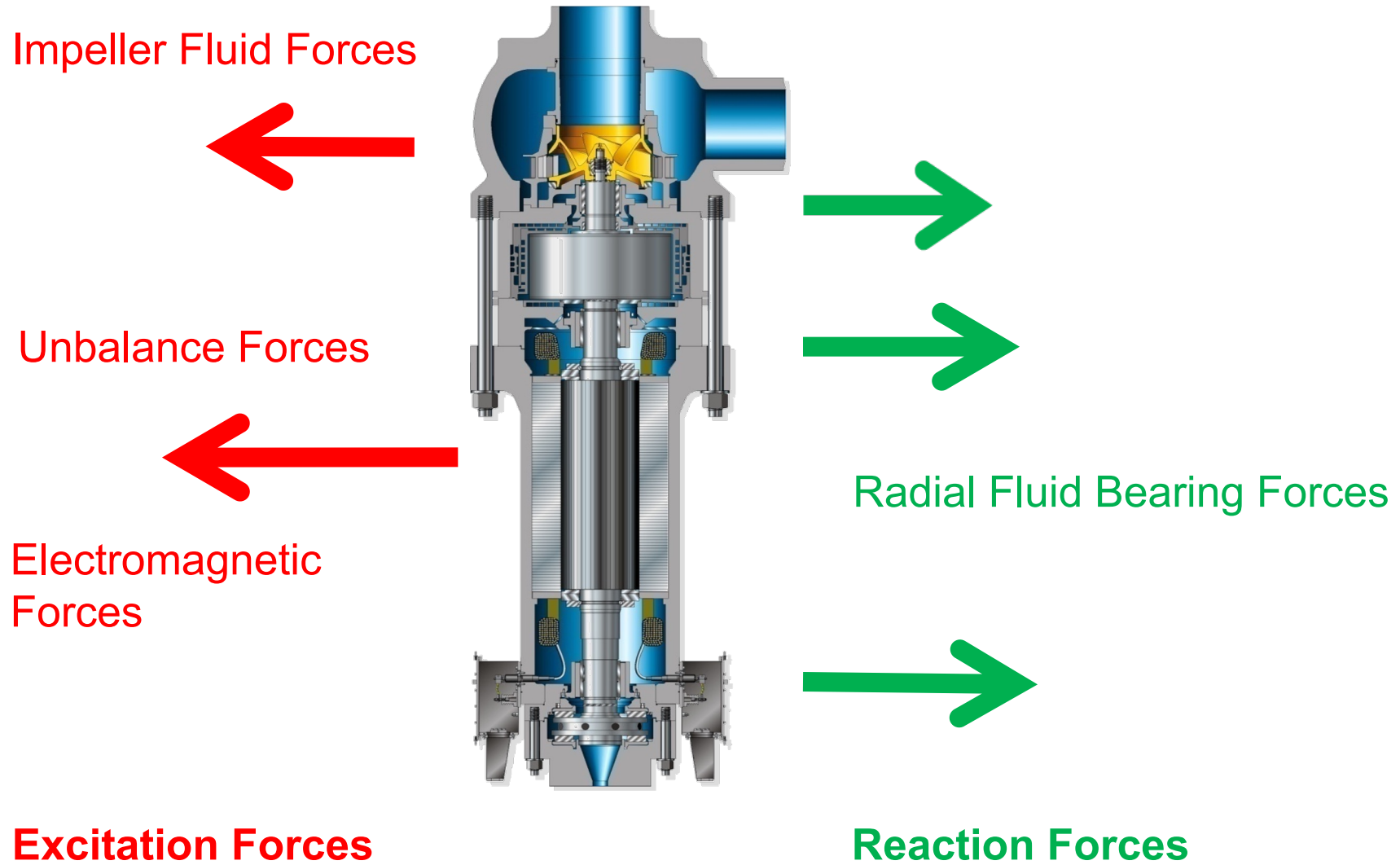
Vibration Phenomena of Pump Systems

Important System Components regarding Vibrations



Vibration Phenomena of Pump Systems

Excitation and Reaction Forces for Lateral Vibrations



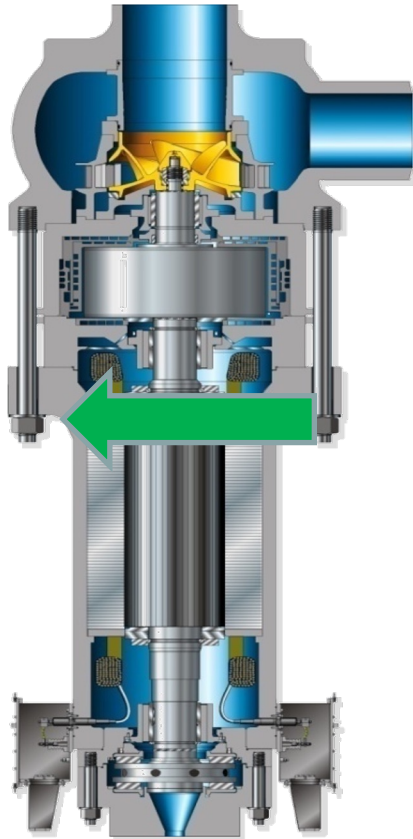
Vibration Phenomena of Pump Systems

Motivation for Rotordynamic Investigations?

- How is the influence of **time dependent forces (moments)** on the dynamic behavior of a Pump System?
- Which **motions of vibration** and which **internal stresses** act on the rotating and on the non-rotating machine parts of the Pump?
- Are critical conditions (**Resonances, Critical Speeds, Instabilities**) possible?
- **Can vibrations destroy machine parts?**
Rubbing, shaft cracks, bearing failures, large deformations,...
- Which **Interactions** have to be considered?
Fluid Structure Interactions FSI (Impeller, bearings, seals),
Rotor Structure Interaction RSI (Pump casing, foundation)
Electromechanical Interaction in the motor drive

Vibration Phenomena of Pump Systems

Lateral Vibrations



Lateral Vibrations: perpendicular to the shaft axis with bending along the shaft line.

Physical Effects: Inertia (masses), stiffness and damping of the system components.

Dynamic Characteristics: Lateral natural frequencies, critical speeds, natural modes, stability, Frequency Response Functions (FRF)

Excitations:

Unbalance forces, excitation with rotational frequency,

Fluid forces at the impeller with vane passing frequency

Electromagnetic forces at the motor

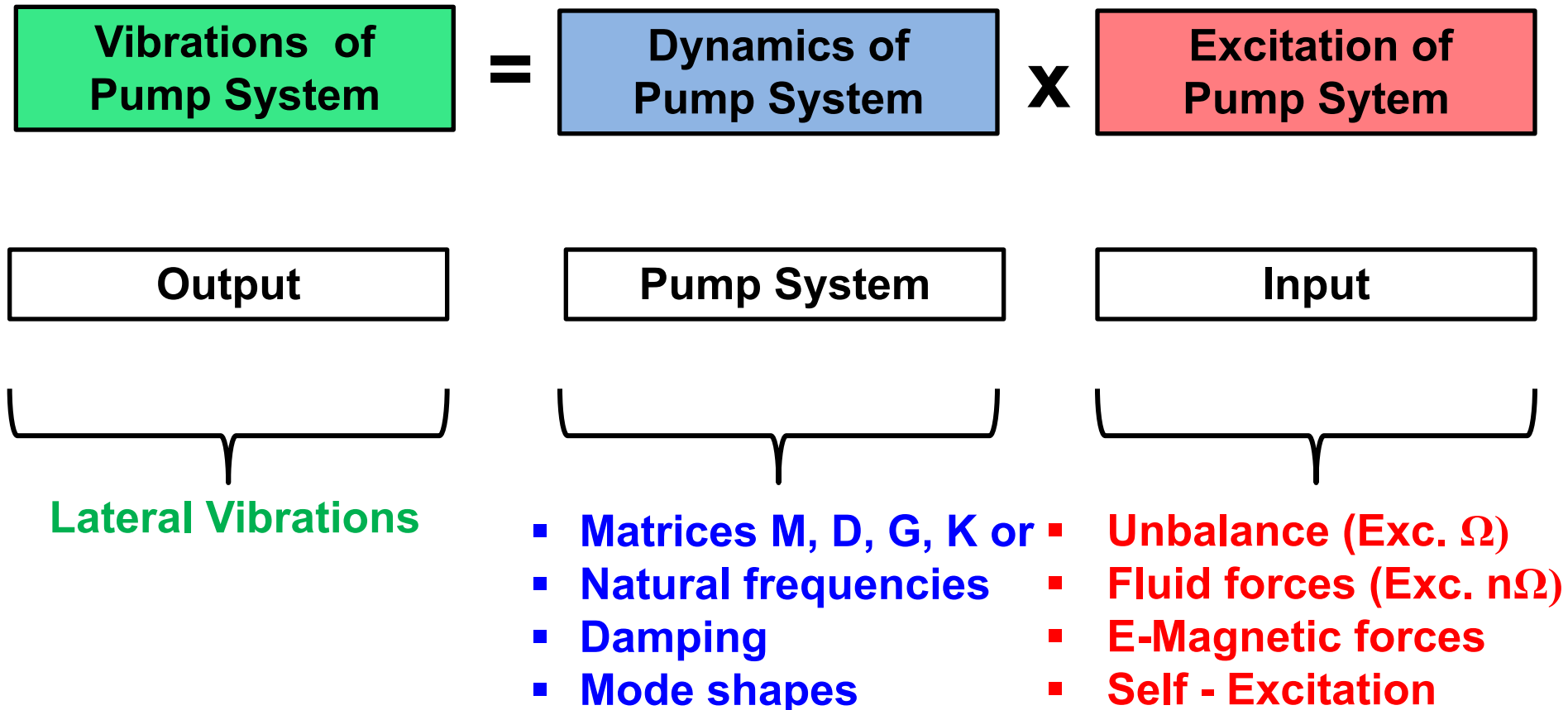
Self excited vibrations, Instability in bearings and seals

Pump Vibrations in Power Plants

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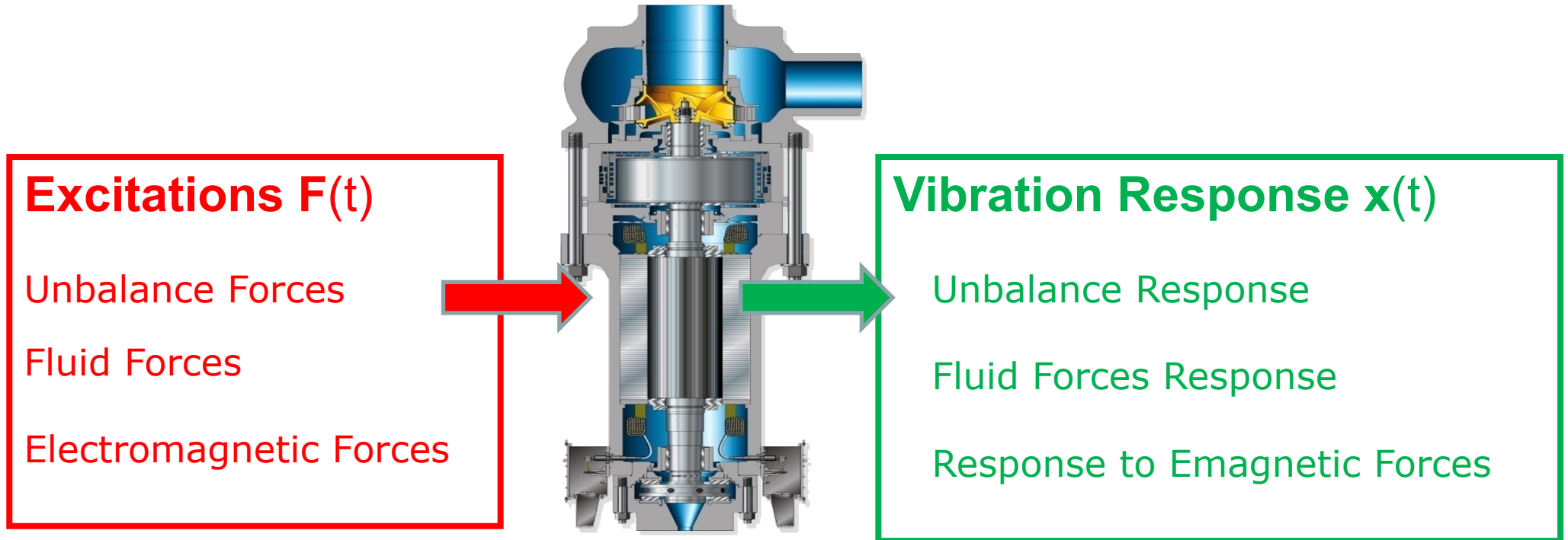
Modelling of Pump Systems to Predict Vibration Phenomena

Equations of Motion - Input Output Relations



Modelling of Pump Systems to Predict Vibration Phenomena

Equations of Motion, Input Output Relations



Dynamic Characteristics of the Pump System:

Physical Parameters: Mass, Damping & Stiffness of Shaft, Fluid Bearings, Seals

Modal Parameters: Natural frequencies, Damping, Natural modes,

Modelling of Pump Systems to Predict Vibration Phenomena

Stiffness and Damping Coefficients of Fluid Film Bearings and Seals

The Forces of **Fluid Film Bearings** and **Seals** can be presented by **stiffness and damping coefficients** k_{ij} and d_{ij} in linear form:

$$F_z(t) = k_{zz}z + k_{zy}y + d_{zz}\dot{z} + d_{zy}\dot{y}$$

$$F_y(t) = k_{yz}z + k_{yy}y + d_{yz}\dot{z} + d_{yy}\dot{y}$$

They depend on the **geometry** (diameter, width, clearance) of the Bearings and Seals, on the **physical fluid data** (density, viscosity, temperature) and on the **operating conditions** (rotational speed, pressure, temperature, ..).

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Modelling of Pump Systems to Predict Vibration Phenomena

Stiffness and Damping Coefficients of Fluid Film Bearings and Seals

The **stiffness and damping coefficients** of Fluid film bearings and Seals can be determined by **Numerical calculations** (CFD) or by **Experiments**.

Example: For a bearing with a special geometry the coefficients depend on the **Sommerfeld number So** . Fluid film bearings have anisotropic behavior :

$$k_{zz} \neq k_{yy} \text{ and } d_{zz} \neq d_{yy}$$

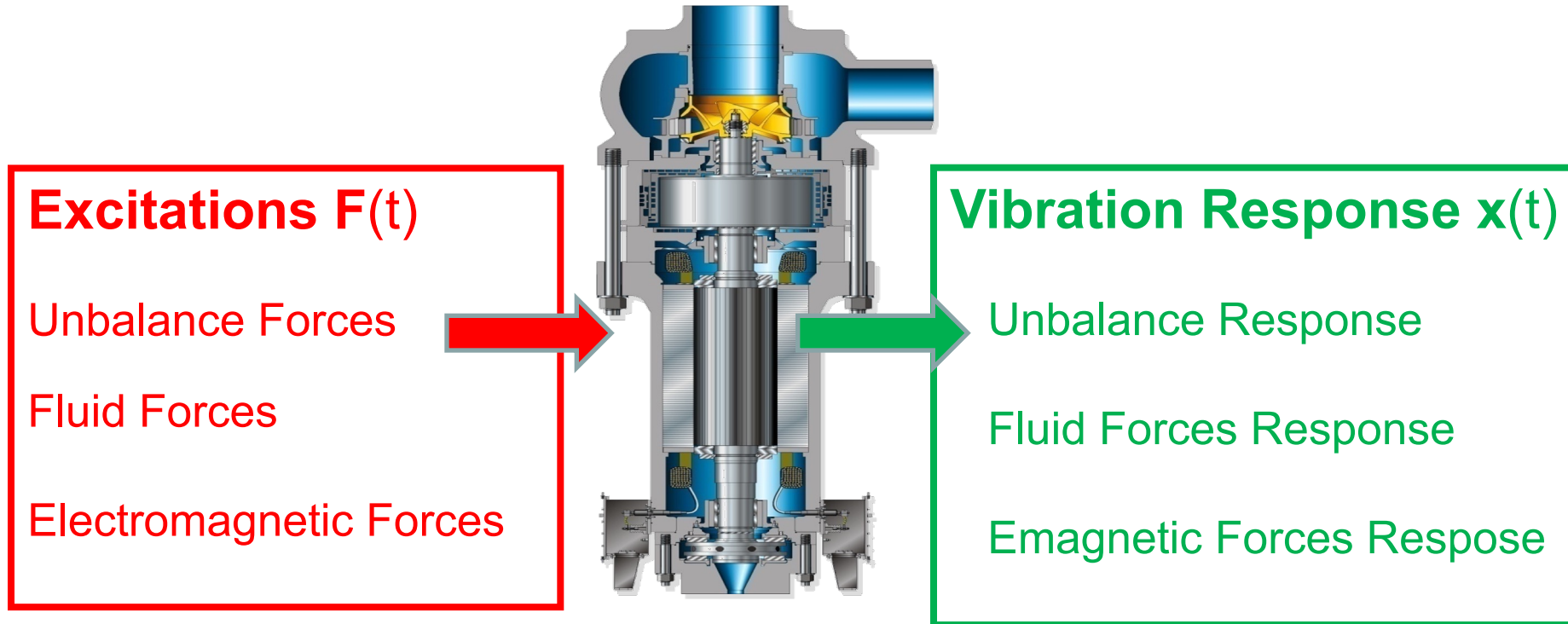
The coupling coefficients differ from each other (unsymmetry):

$$k_{zy} \neq k_{yz} \text{ and } d_{zy} \neq d_{yz}$$

A measure for **instability sensitivity** is the difference: $(k_{zy} - k_{yz})$.

Modelling of Pump Systems to Predict Vibration Phenomena

Equations of Motion, Input Output Relations

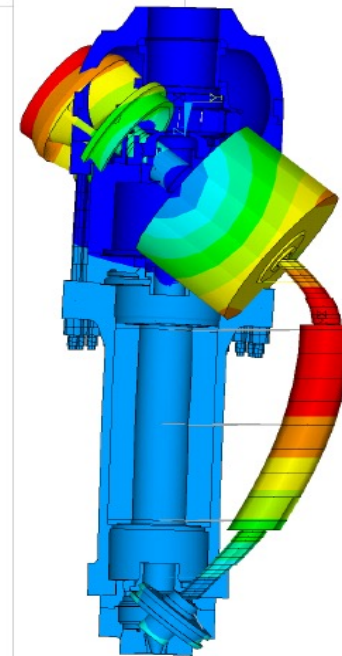
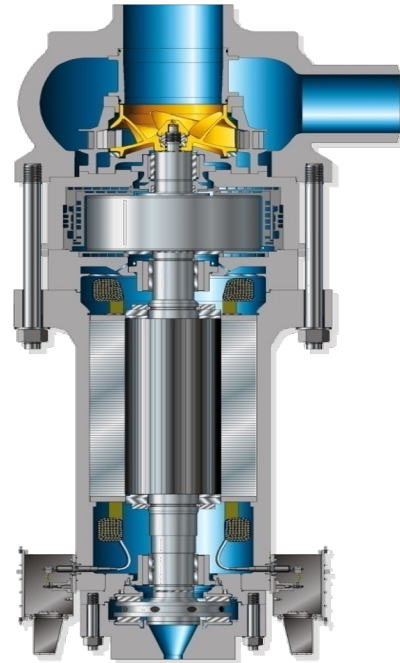


$$\mathbf{M} \ddot{\mathbf{x}}(t) + (\mathbf{D}(\Omega) + \mathbf{G}(\Omega)) \dot{\mathbf{x}}(t) + \mathbf{K}(\Omega) \mathbf{x}(t) = \mathbf{F}(t)$$

The **Equations of Motion of the Pump** contain the stiffness & damping & mass information of the shaft and the bearings and seals. The dynamic influences of the **casing** and the **pipng** can be included.

Modelling of Pump Systems to Predict Vibration Phenomena

Natural Vibrations: Eigenvalues and Mode Shapes



Natural frequency ω

Damping α

Bending mode

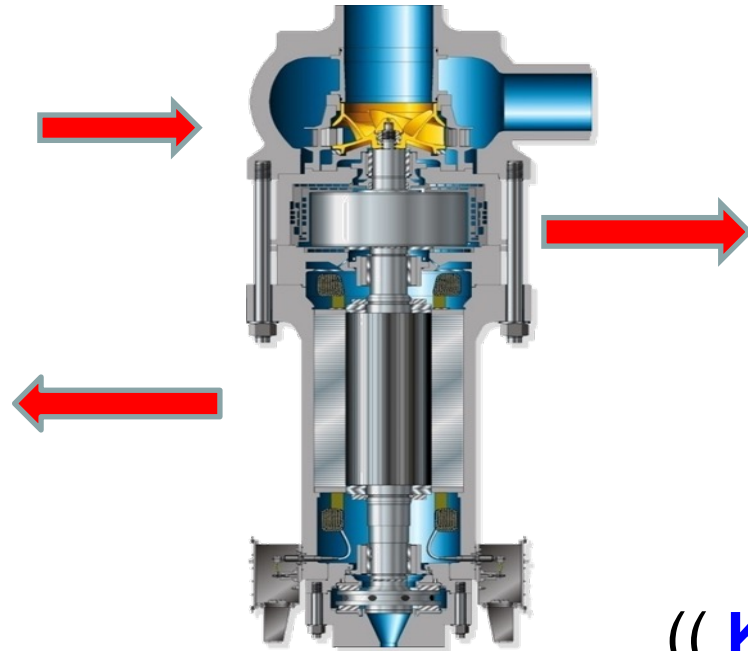
$$(\lambda^2 \mathbf{M} + \lambda(\mathbf{D}(\Omega) + \mathbf{G}(\Omega)) + \mathbf{K}(\Omega)) \cdot \mathbf{x} = 0$$

Complex Eigenvalues : $\lambda = \alpha + j \omega$

Information for **natural frequencies** ω and **damping** α (stability)

Modelling of Pump Systems to Predict Vibration Phenomena

Lateral Vibrations due to **Unbalance Forces**



Unbalance forces act mainly at the main masses m : impeller, flywheel and motor. For each mass they are defined by **amplitude** $me\Omega^2$ and **phase**

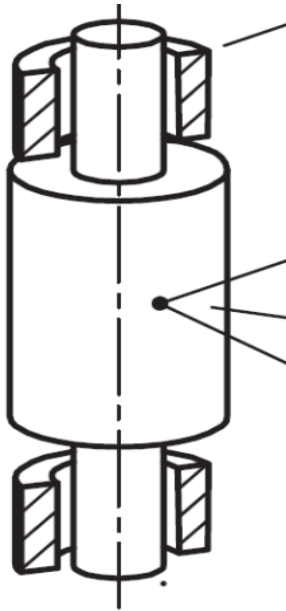
$$((\mathbf{K}(\Omega) - \Omega^2 \mathbf{M}) + j\Omega (\mathbf{D}(\Omega) + \mathbf{G}(\Omega)) \mathbf{x} = \mathbf{U} \Omega^2 \mathbf{F}_i$$

Complex System response \mathbf{x}_i contains amplitude and phase

Modelling of Pump Systems to Predict Vibration Phenomena

Lateral Vibrations due to **Unbalance Forces and Instability**

This prestudy investigates the lateral **vibrations of a rigid mass m with unbalance**, running with **angular velocity Ω** in cylindrical hydrodynamic **waterfilm bearings**. The shaft arrangement is vertical



Hydrodynamic circular **waterfilm bearing 1**

Mass of Impeller m

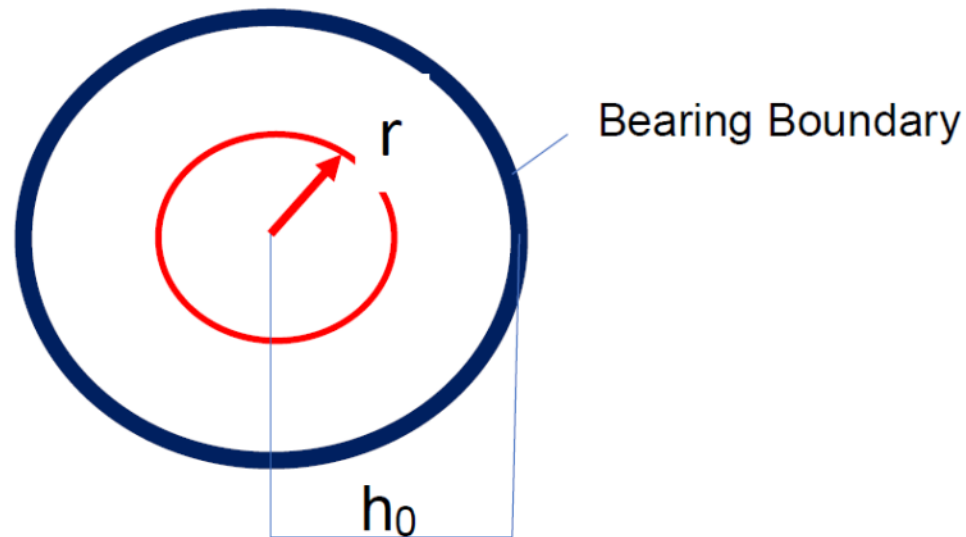
Mass eccentricity: ε

Hydrodynamic circular **waterfilm bearing 2**

Modelling of Pump Systems to Predict Vibration Phenomena

Lateral Vibrations due to **Unbalance Forces and Instability**

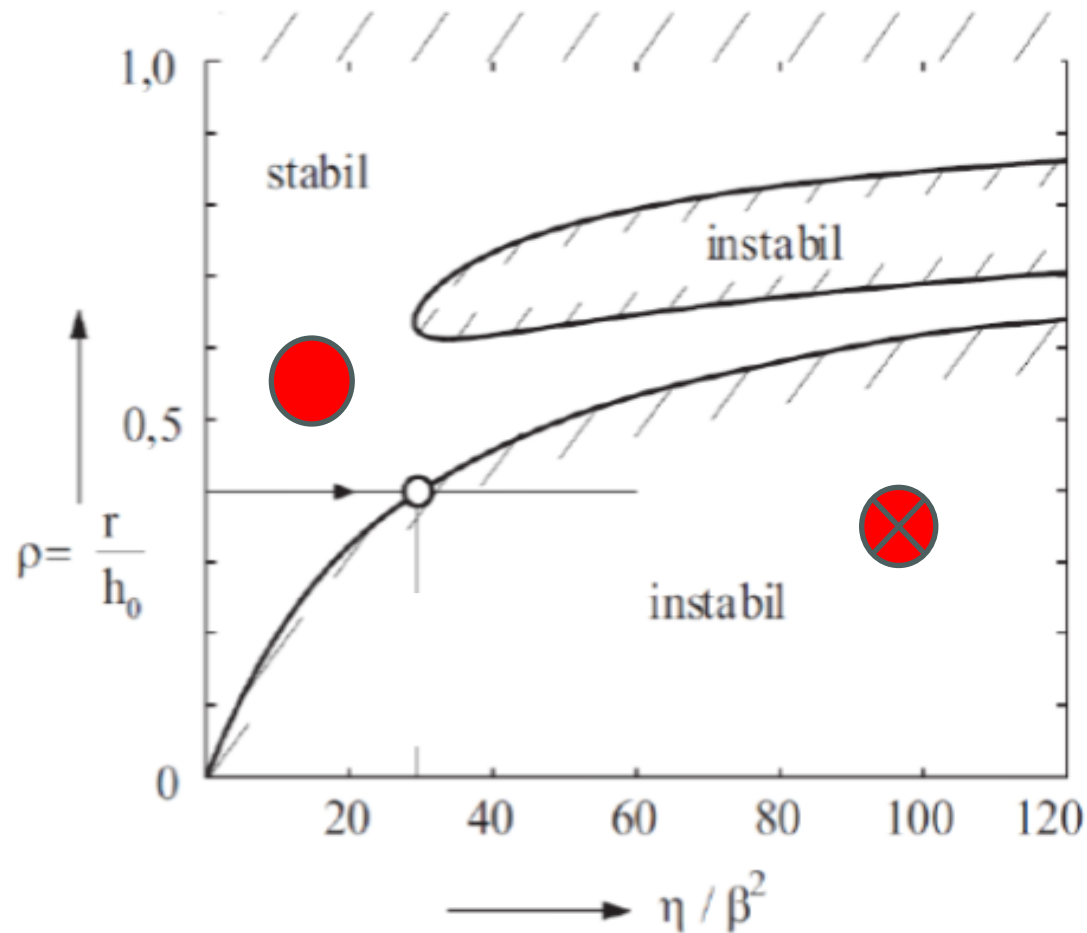
With a **nonlinear calculation** for the impeller mass m and the circular waterfilm bearing we can determine **the vibration amplitude r of an circular orbit** due to an **unbalance ε** acting at the impeller. **The frequency of the orbit is Ω** . The amplitude r can be related to the radial bearing clearance h_0 , where ρ is between 0 and 1.



$$\rho = r / h_0 < 1$$

Modelling of Pump Systems to Predict Vibration Phenomena

Lateral Vibrations due to **Unbalance Forces and Instability**



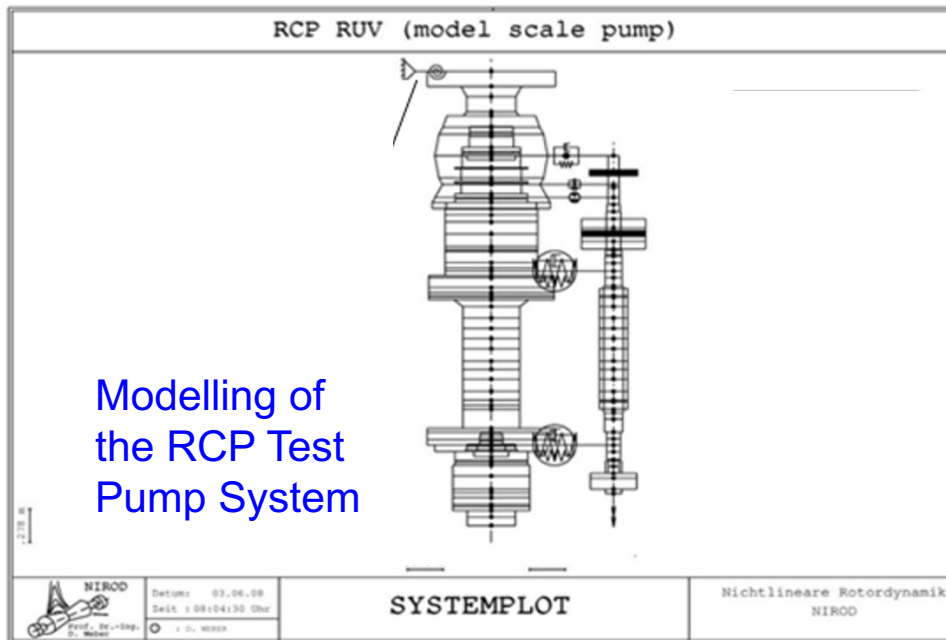
This diagram shows, that **stable and unstable** motions are possible.

Are we in a stable or unstable range?

Subsynchronous vibrations will appear in the unstable range.

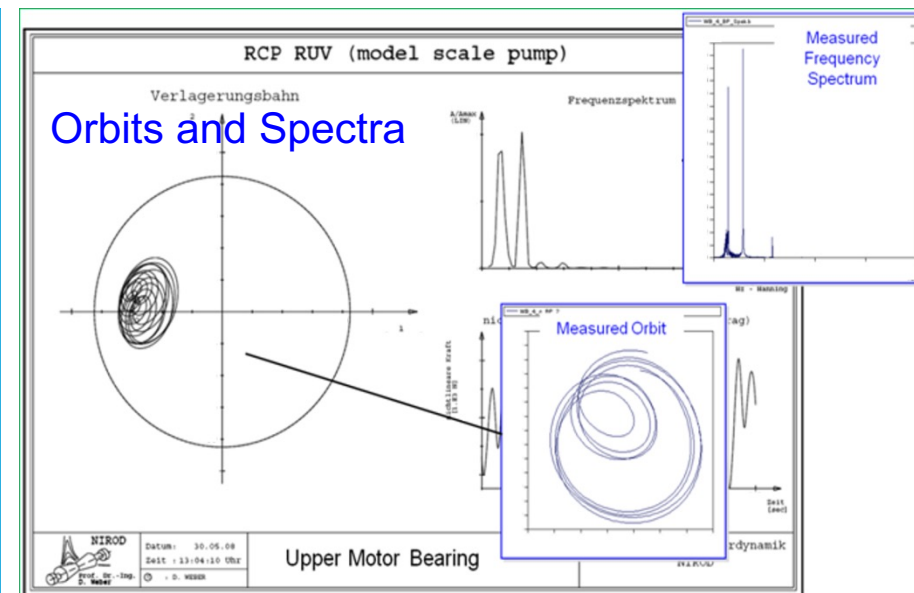
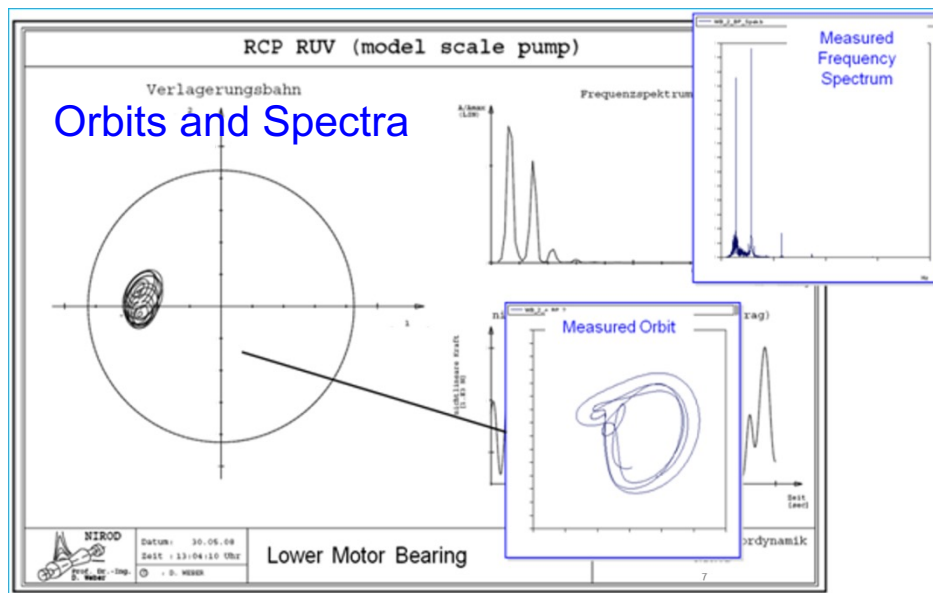
A final solution has to be found numerically.

High Unbalance Forces stabilize!



Lateral Vibrations of a Test Pump System

Unbalance Vibrations with shaft rotational frequency Ω and **unstable vibrations** with $\sim \Omega/2$ (**whirl**).
 Calculated and measured **Orbits** and **Frequency Spectra** at the lower and upper motor bearing.

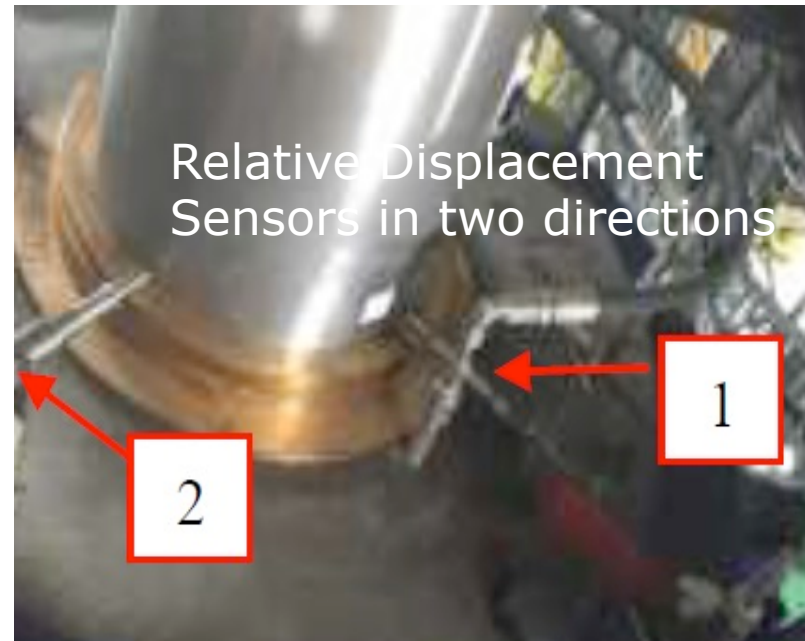
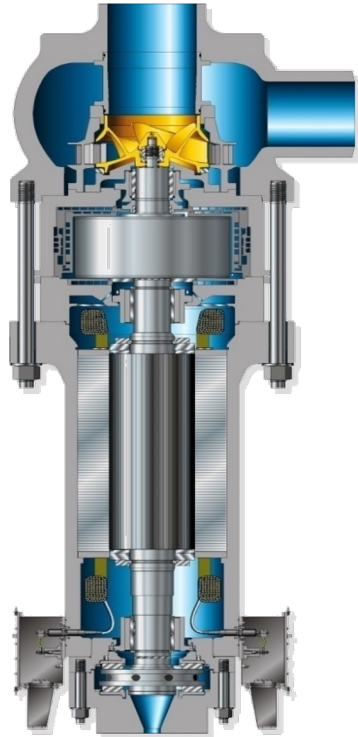


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Monitoring of Pump Systems for Vibration Control

Monitoring by means of Relative Displacement Sensors

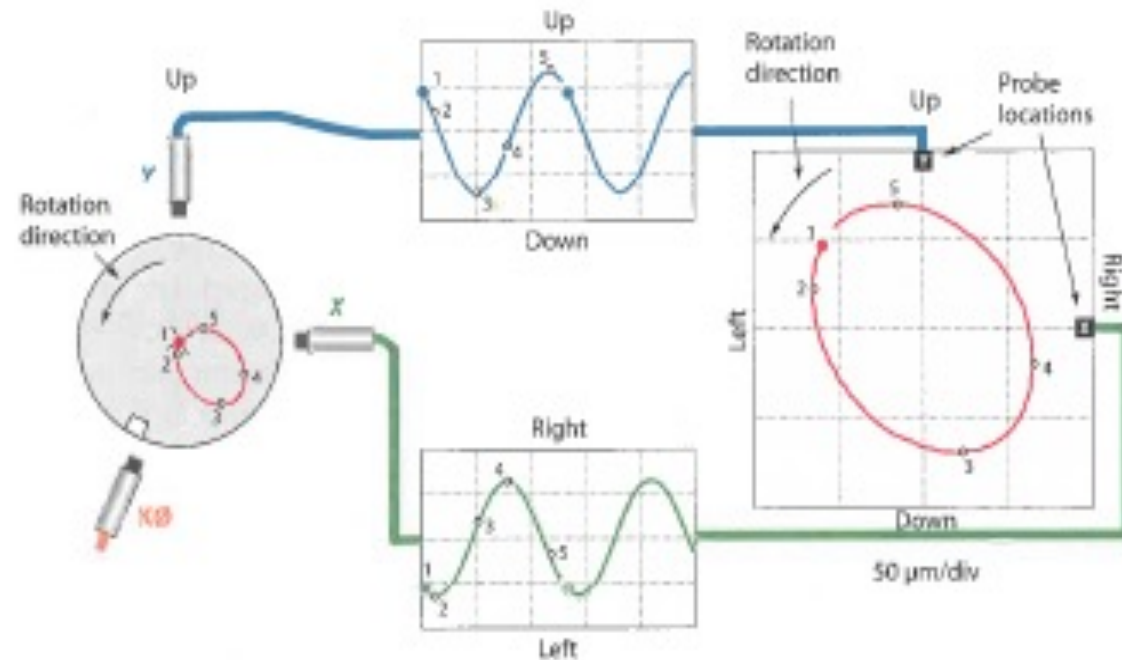


For Monitoring of Pump Systems **absolute vibration velocities in mm/sec** and/or **relative shaft vibrations in μm** at defined locations (Bearings) are usually measured. Vibrations are evaluated e.g. by ISO Standards or other Standards.

Monitoring of Vertical Pump Systems

Conventional Monitoring

Measurement of **relative shaft vibrations** in horizontal and vertical direction by means of displacement sensors. By superposition of the two signals in one plane **Orbits** can be determined. They show the **shaft motions** in the measurement plane.

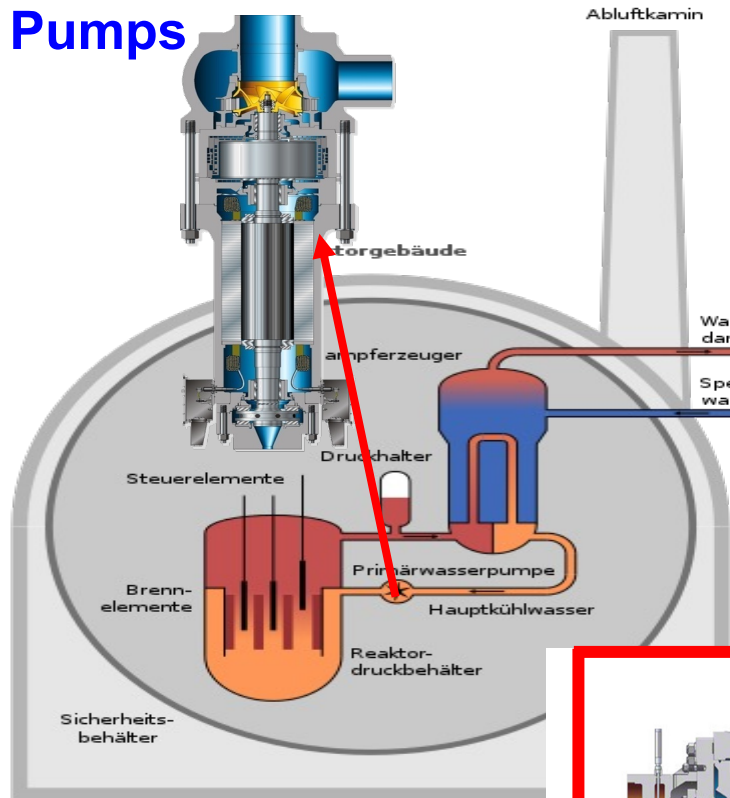


Pump Vibrations in Power Plants

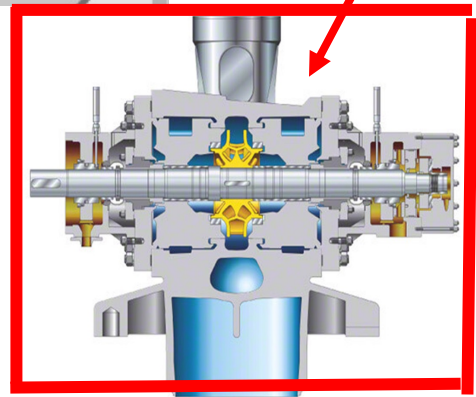
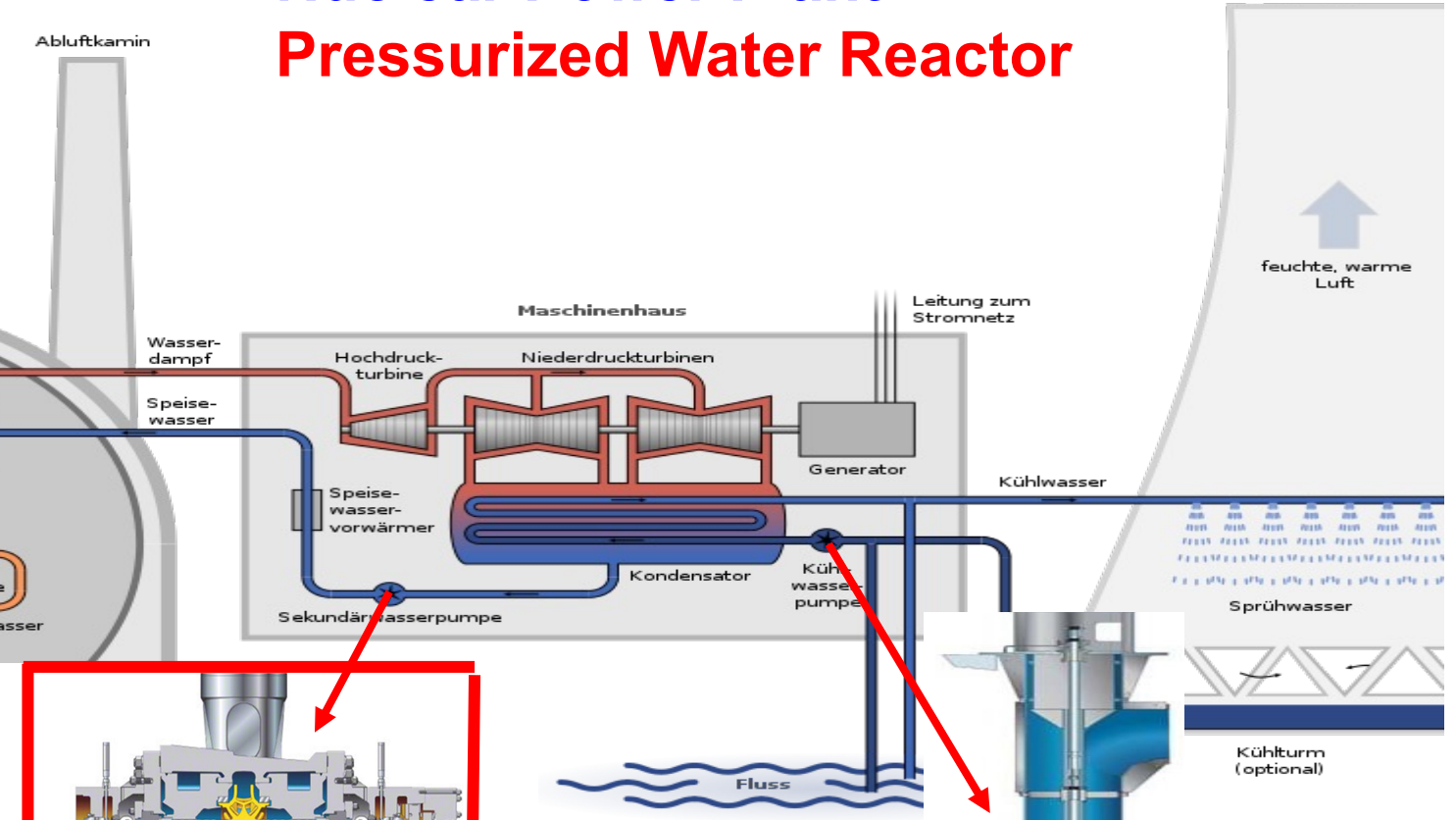
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Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Vertical Reactor Coolant Pumps



Nuclear Power Plant Pressurized Water Reactor

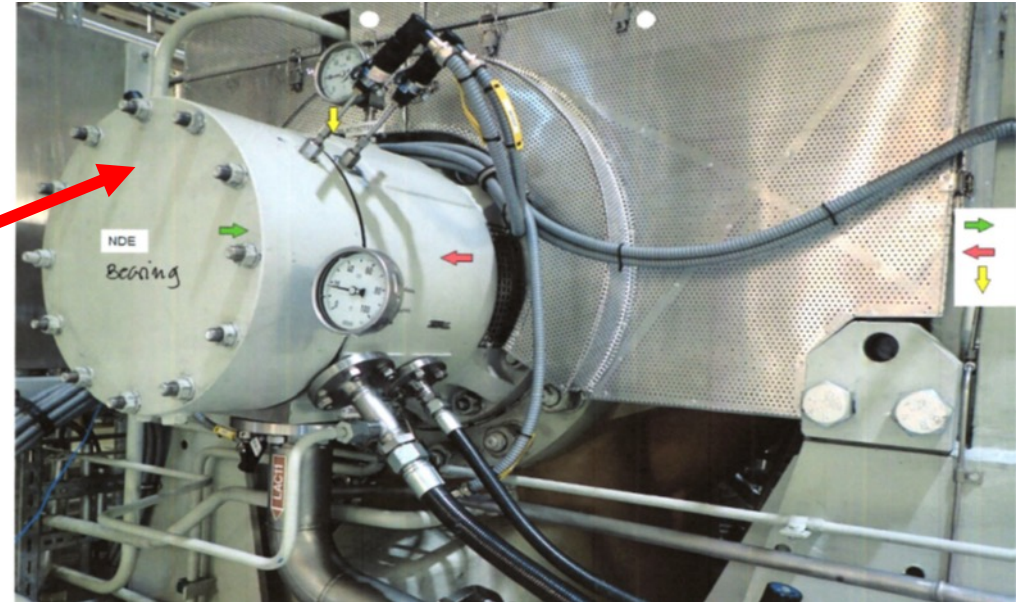
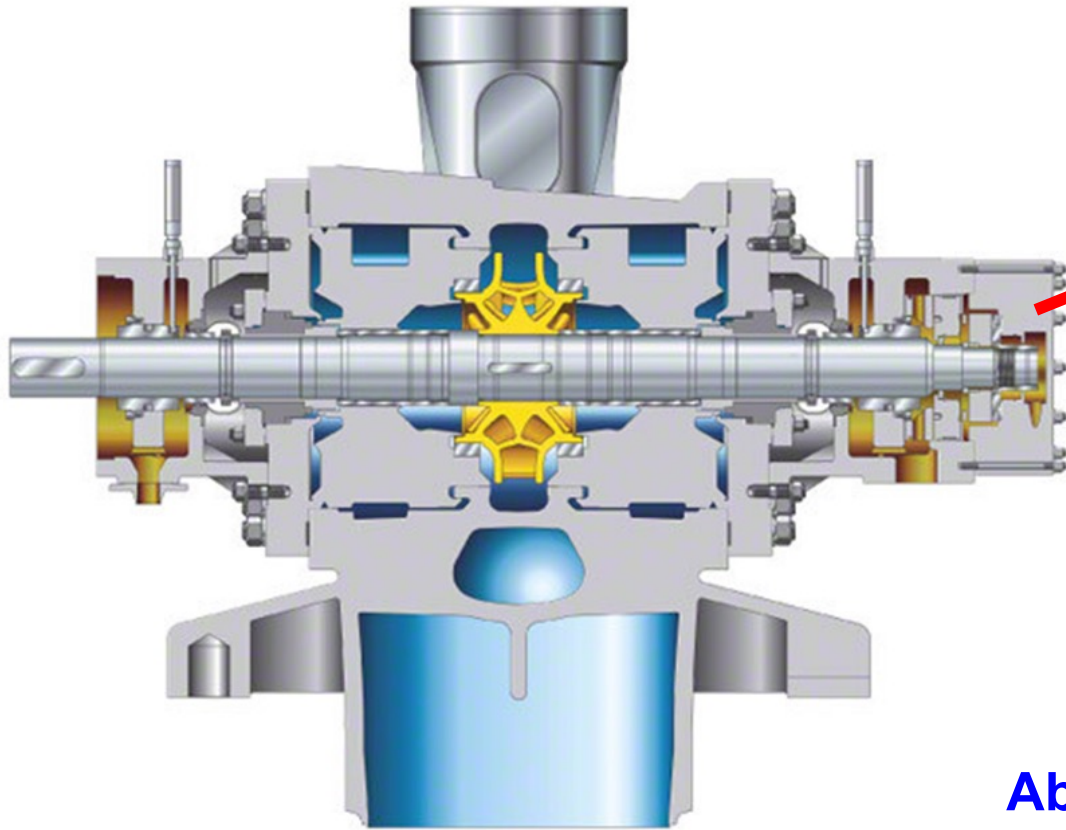


Horizontal Boiler Feed Pump



Vertical Cooling Water Pump

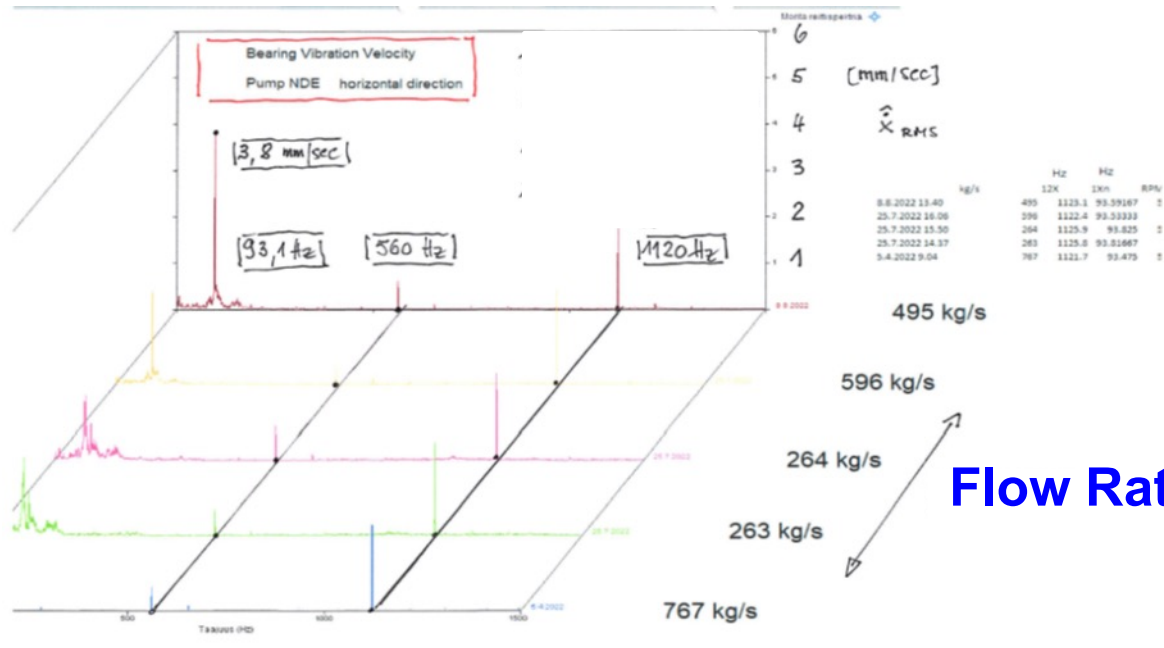
Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces



Absolute RMS Vibration velocities \dot{x}_{RMS} were determined at the two **Bearing housings** in horizontal, vertical and axial directions

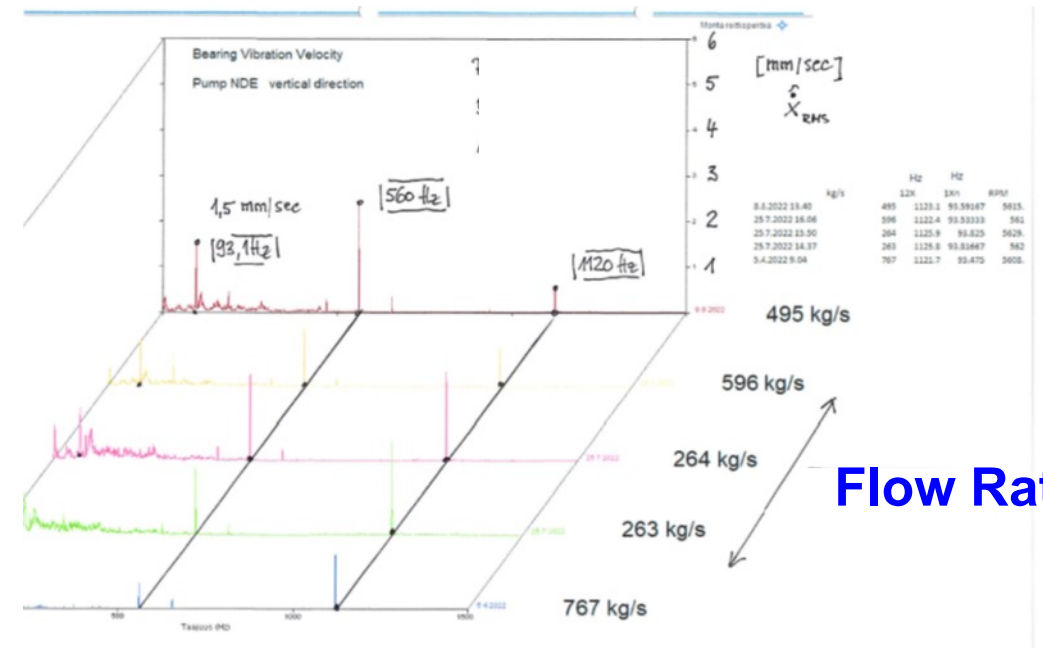
Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

NDE Bearing horizontal \dot{x}_{RMS}



560 Hz 1120 Hz

NDE Bearing vertical \dot{x}_{RMS}



560 Hz 1120 Hz ⇒ Frequency Hz

Flow Rate

Flow Rate

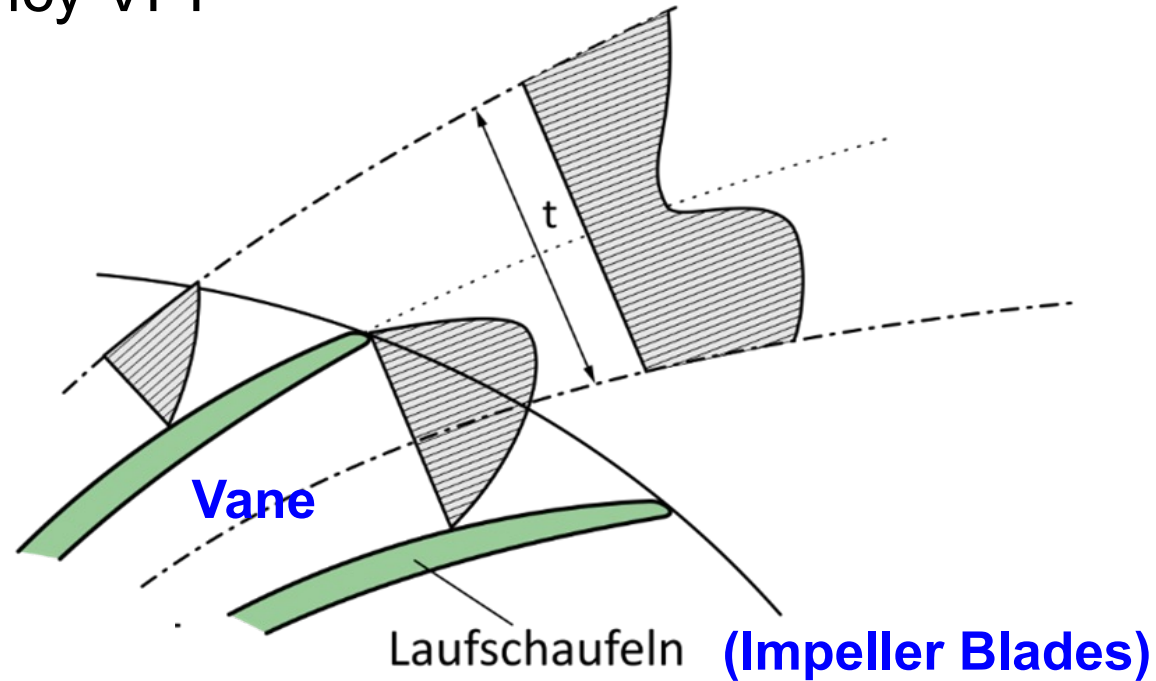
495 kg/s
596 kg/s
264 kg/s
263 kg/s
767 kg/s

495 kg/s
596 kg/s
264 kg/s
263 kg/s
767 kg/s

How can the **vibrations** at **frequencies of 560 Hz and 1120 Hz** be explained ?

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Vane Pass Frequency VPF



The Fluid Structure Interaction creates **Fluid Forces** in the area between the **impeller** and **the volute** with the blade passing frequency **$VPF = f_{rot} \times N$** and higher Harmonics of it. **$f_{rot} = \Omega / 2\pi$** is the rotational frequency of the pump shaft in Hz and N is the number of blades.

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Campbell Diagram with Excitation lines and Natural Frequencies

In case of the considered **Boiler Feed Pump**

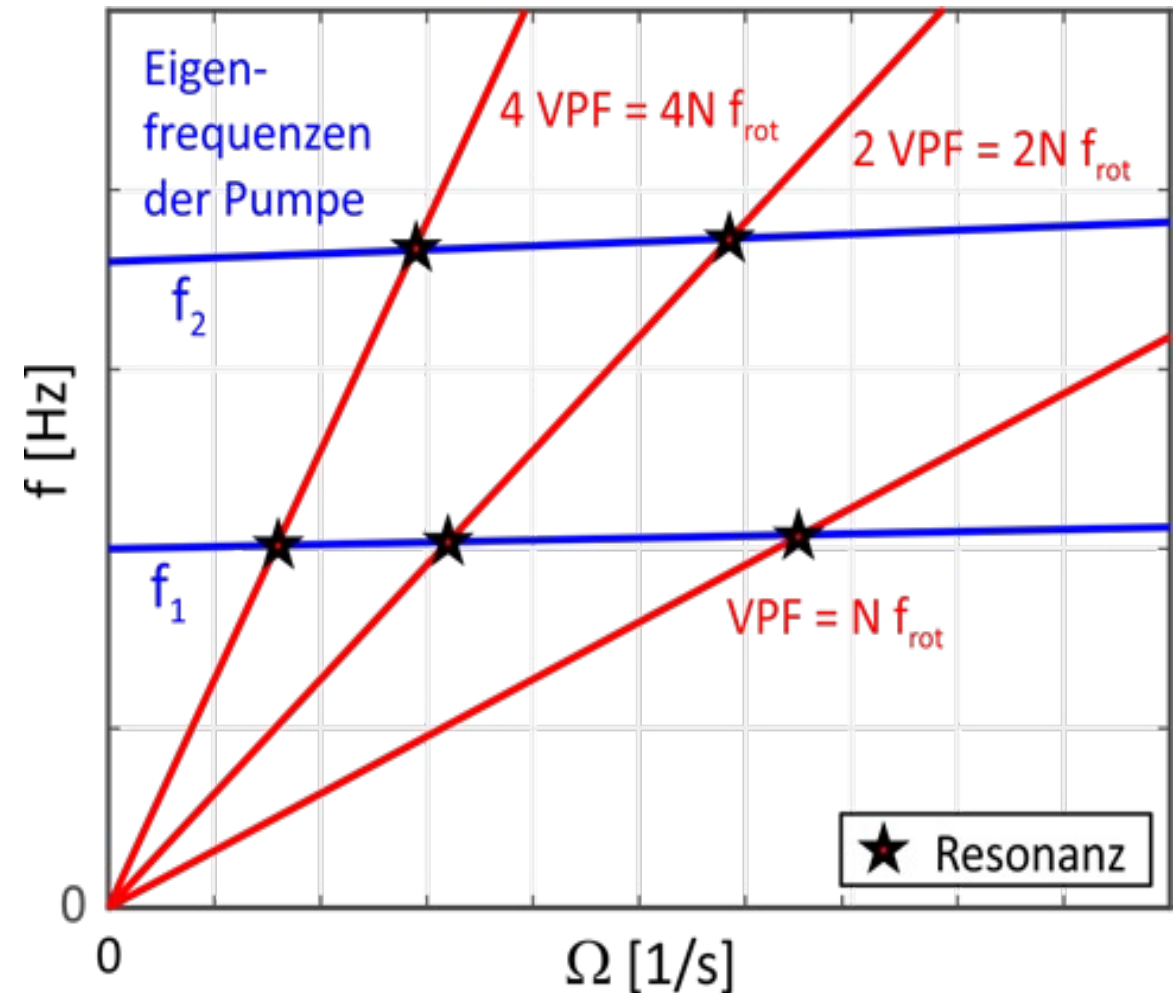
$$f_{\text{rot}} = 93,2 \text{ Hz} \quad \text{and} \quad N = 6$$

and the **Vane Passing Frequency VPF** is

$$\text{VPF} = 560 \text{ Hz} \quad \text{and} \quad 2 \text{ VPF} = 1120 \text{ Hz}$$

In a **Campbell Diagram** we can find possible **Resonances**, when the speed dependent **Excitation Frequencies VPF, 2 VPF, ...** cross the speed dependent **lateral natural frequencies** (blue lines) of the pump system.

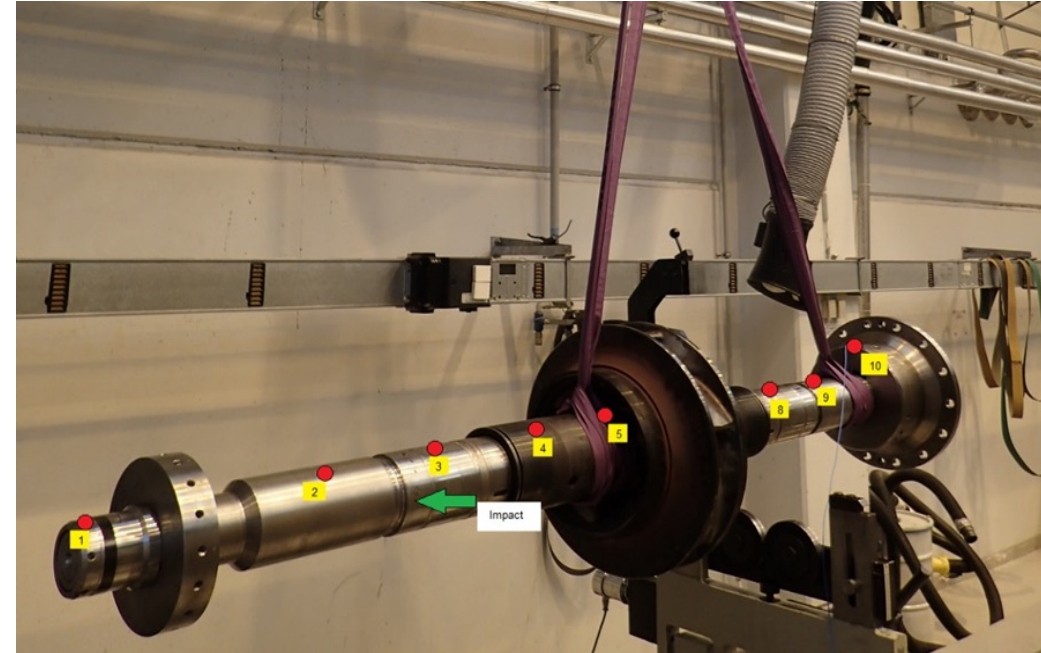
To find the **Resonances** the **lateral natural frequencies** have to be determined.



Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Determination of the Lateral Natural Frequencies by Exp. Modal Analysis

- **Test Set Up for Exp. Modal Analysis**
 - Pump shaft with Masses and Moments of Inertia of impeller, coupling and axial bearing in free free condition
 - No bearings, no seals
 - No rotation of shaft



Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

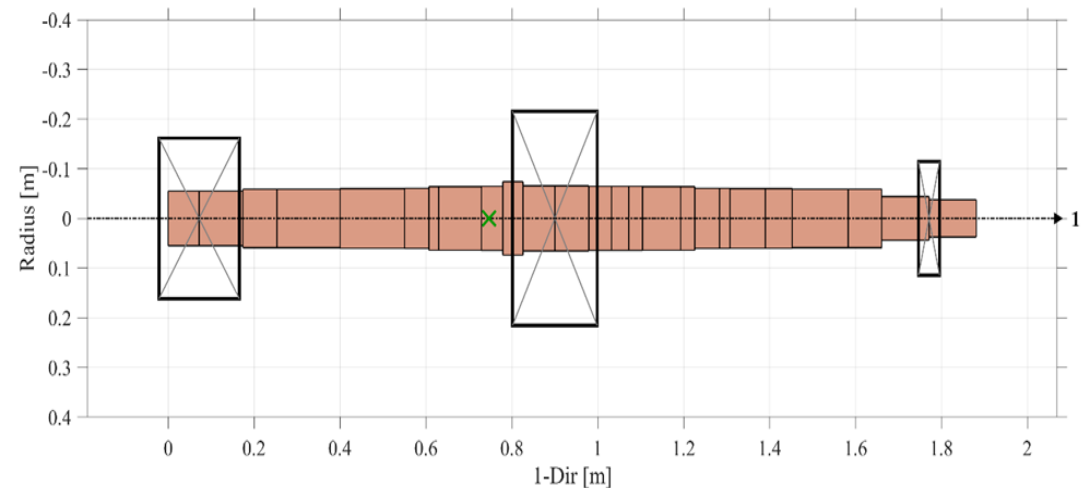
Determination of the Lateral Natural Frequencies by a FE - Model

- The FE Model consists of
 - Pump shaft (stiffness and mass of shaft)
 - Masses and Moments of Inertia of impeller, coupling and axial bearing
 - No bearings, no seals
 - No rotation of shaft

Total mass: 317.88 kg, CoG: 747 mm
Polar moment of inertia: 2.9893 kg m²
Transverse moment of inertia: 91.102 kg m²
Nominal speed: 50.00 rps, 3000 rpm



Shaft 1

— ODi main
— IDi main
— ODs main
— IDs main
— OD add mass/inert



Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Calculated and measured Lateral Natural Frequencies of free-free pump shaft

	MADYN-Result	Modal Analysis Measurement (TVO)	Deviation
1. Natural frequency	0,0 Hz	0 Hz	
2. Natural frequency	0,0 Hz	0 Hz	
3. Natural frequency	108,6 Hz	104,7 Hz	+3,7 %
4. Natural frequency	309,5 Hz	304 Hz	+1,8 %
5. Natural frequency	 533,1 Hz	541 Hz	-1,5 %
6. Natural frequency	772,5 Hz	791 Hz	-3,4 %
7. Natural frequency	 1105,8 Hz	1126 Hz / 1154 Hz	-1,8 % / -4,3 %
8. Natural frequency	1379,9 Hz	1300 Hz	+6,1 %



Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Lateral Natural Frequency and Mode Shape at 533 Hz

Eigenvalue Analysis

Analysis: 01-Nov-2022 10:30:02 - bearing loads ignored

Relative speed: 0%

Shafts: 1

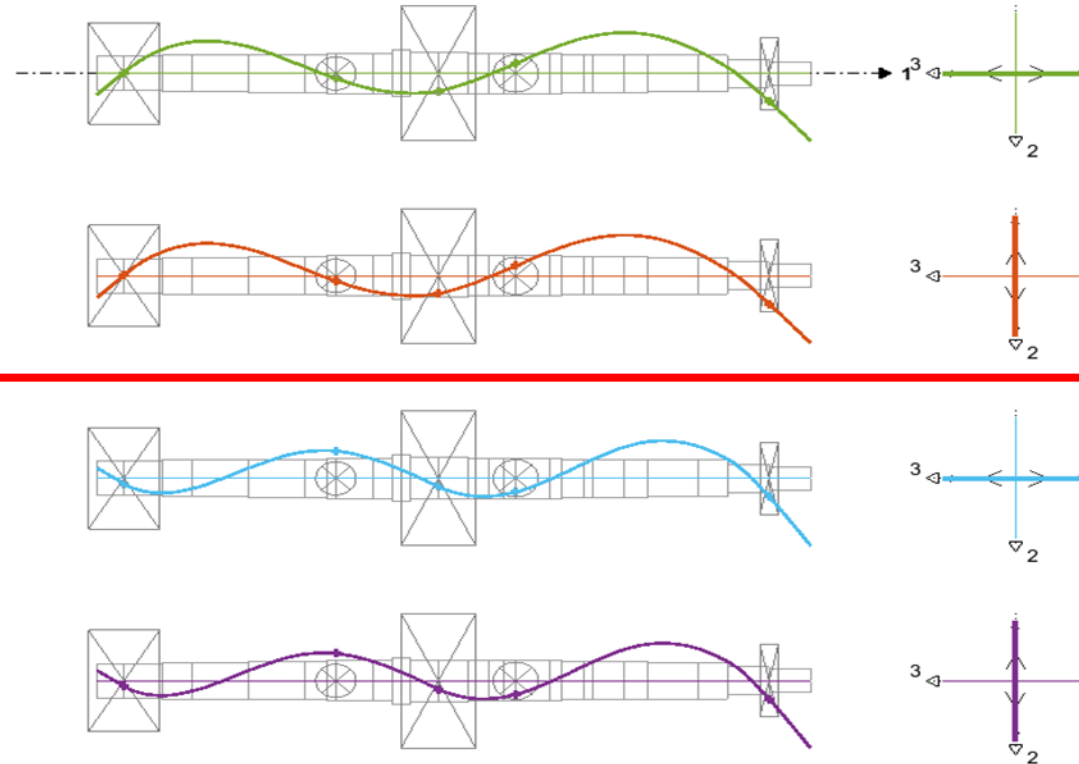
Mode: 9
Frequency: 533.13 Hz
31988.1 cpm
Damping Ratio: 0.0 %
Whirling direction: +0.00

Mode: 10
Frequency: 533.14 Hz
31988.1 cpm
Damping Ratio: -0.0 %
Whirling direction: +0.00

Mode: 11
Frequency: 772.51 Hz
46350.6 cpm
Damping Ratio: -0.0 %
Whirling direction: +0.00

Mode: 12
Frequency: 772.51 Hz
46350.6 cpm
Damping Ratio: 0.0 %
Whirling direction: +0.00

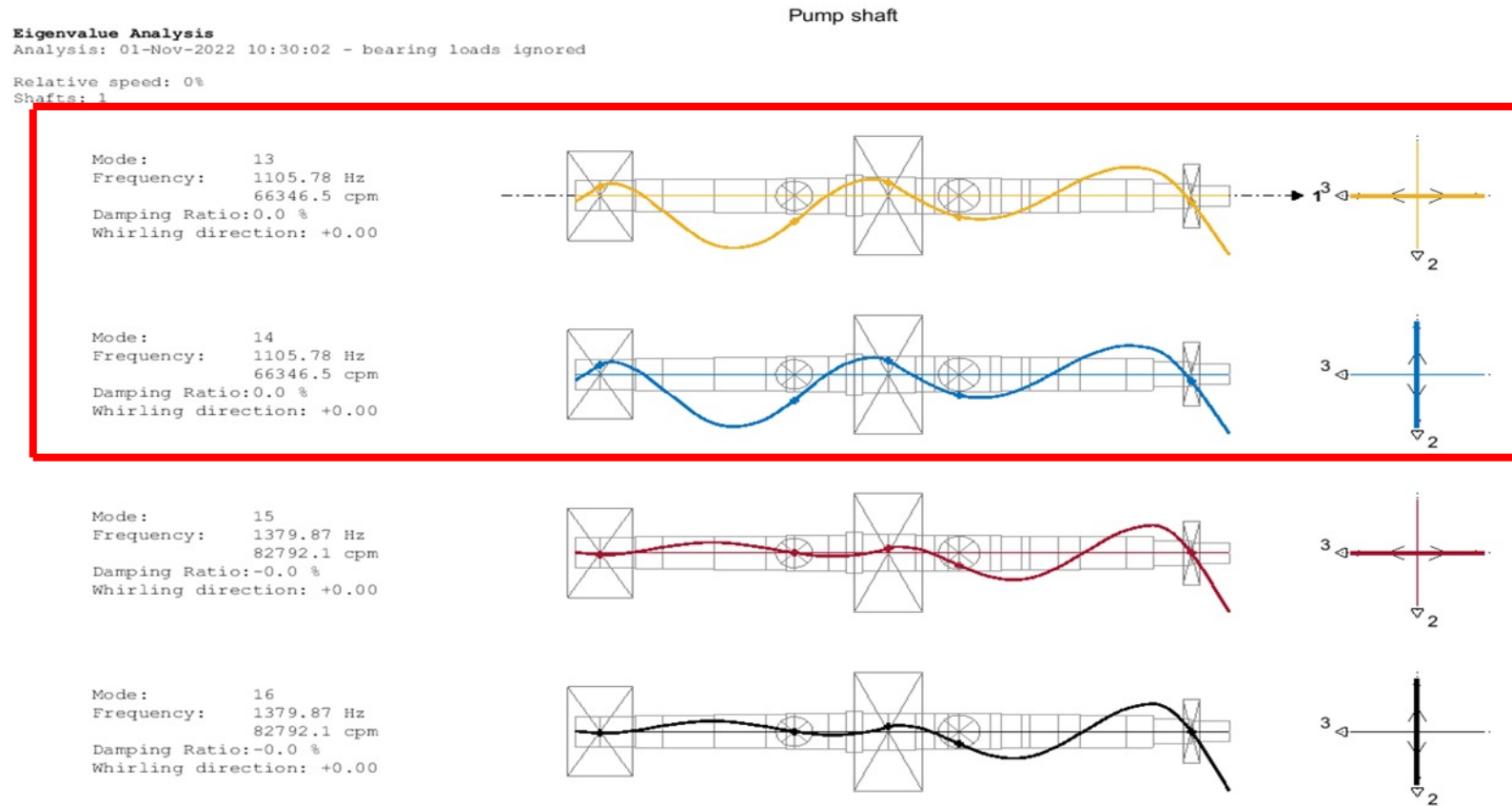
Pump shaft



533 Hz

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Lateral Natural Frequency and Mode Shape at 1105 Hz



1105 Hz

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Further Investigations of this Pump Vibration Problem

Further investigations of the **Dynamic behaviour of the Boiler Feed Pump** have shown:

- The **lateral natural frequencies** of the **free-free Pump shaft** did not change very much, when the full system with **Fluid Film Bearings, Seals and Shaft Rotation** has been considered
- The **Fluid Force Excitation** with the frequencies **VPF = 560 Hz and 2 VPF = 1120 Hz** leads to **Resonances of the Pump System**, mainly due to the Pump shaft dynamics. (see Campbell diagram). This may lead to **contacts** between **the rotating and the nonrotating components** (Bearings and Seal)
- It is difficult to determine the size of the **Fluid Force Amplitudes. Formulas** based on **Experimental Data** from the Literature can be used for an **Estimation of the Fluid Force.** The next slides show, how they can be used.

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Estimation of Fluid Forces

Estimation of Fluid Forces at the Impeller

It is customary to represent **hydraulic excitation forces** in term of a **normalized force coefficient**, defined as follows:

$$K_H = F_H / (\rho \cdot g \cdot H \cdot D_2 \cdot B_2)$$

where:

K_H = normalized hydraulic force

F_H = actual hydraulic force (lbf)

ρ = fluid density (lbf-sec²/in⁴)

g = gravitational acceleration (in/sec²)

H = head generated by impeller stage (in)

D_2 = impeller outside diameter (in)

B_2 = impeller discharge width including shrouds (in)

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Estimation of Fluid Forces

Estimation of Fluid Forces at the Impeller

- The **formula** can be used to calculate different types of **Hydraulic Radial Forces**, acting at the impeller e.g. **Hydraulic Unbalance Forces**, Hydraulic Forces for **Vane Passing Frequencies**, etc....).
- To determine the size of the **Hydraulic Forces F_H** , the **factor k_H** has to be known for the different types of Forces. These values can be found in a paper from Florjancic and Frei. They depend on the **frequency of the Hydraulic Force** and on the **Flow rate Q/Q_{opt}**
- In case of the **Boiler Feed Pump** the **Vane Pass Frequencies VP1 and VP2** are dominant. Values for this type of Hydraulic Force can be taken from the diagram.

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Estimation of Fluid Forces

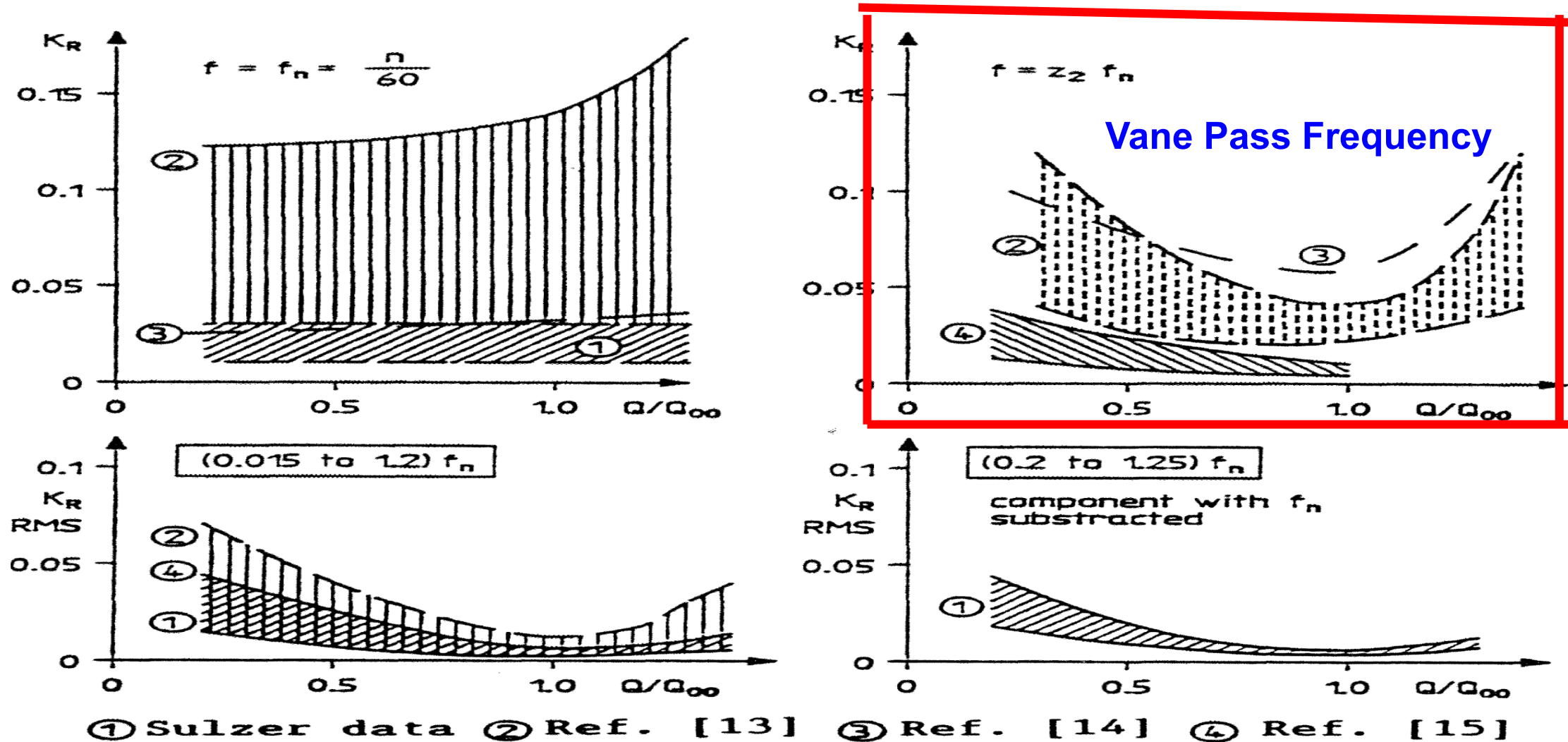
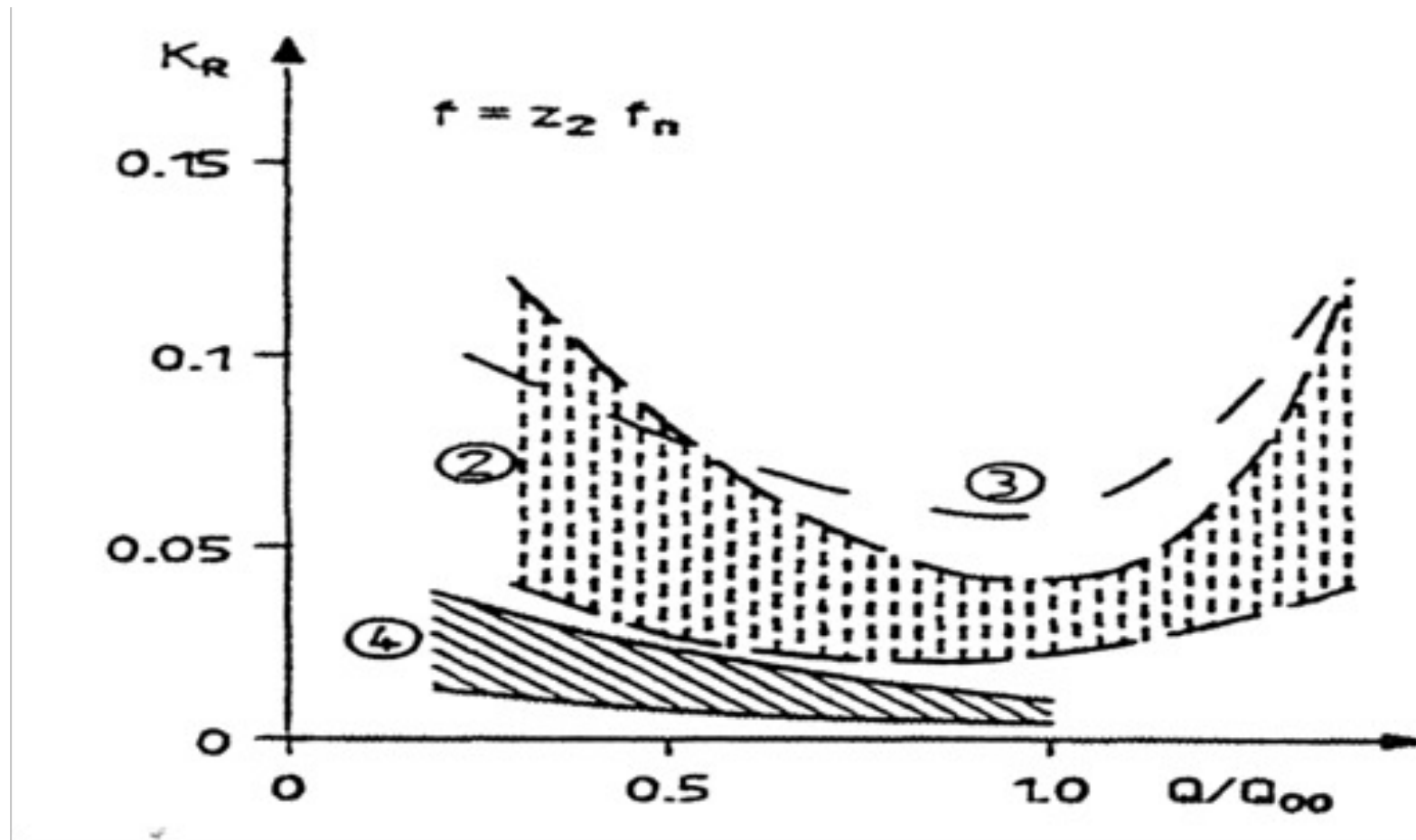


Figure 5. Hydraulic Lateral Excitation Forces.

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Estimation of Fluid Forces for the case of Vane Pass Frequency



Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Estimation of Fluid Forces for the case of Vane Pass frequency

Man findet für

den Optimalpunkt $Q/Q_{opt} = 1$: $KH = 0,05$

den Teillastbereich, z.B. $Q/Q_{opt} = 0,3$: $KH = 0,10$

Wenn man damit die Hydraulischen Kräfte FH für den Optimalpunkt und für den Teillastbereich berechnet, so erhält

den Optimalpunkt $Q/Q_{opt} = 1$: $FH = 17,25$ kN

den Teillastbereich, z.B. $Q/Q_{opt} = 0,3$: $FH = 34,50$ kN

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Conclusions

- Vibrations of the **Boiler Feed Pump** can strongly be excited by **Fluid Forces with Vane Pass Frequency VPF** and Harmonics (e.g. 2 VPF). **Resonances** may occur at this Frequencies (see Campbell diagram).
- Under special **flow conditions** Fluid Forces at the impeller are **synchronous** to the **rotating frequency** of the shaft.
- This **hydraulic forces** behave the same way as a **mechanical unbalance**. **Hydraulic Unbalance forces** are caused by deviations from **rotational symmetry** of the **fluid flow through the impeller** channels (different blades and vanes, geometrical inequality, material roughness, cavitation, unequal energy transfer).

Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces

Conclusions

- **Verhoeven** (1988) states that the **unbalance forces** observed in practical pumps **almost always exceed** those that can be attributed to **mechanical unbalance**. The cause of this discrepancy is **hydraulic unbalance forces**, which he states are usually **much larger than those due to mechanical unbalance**.

Pump Vibrations in Power Plants

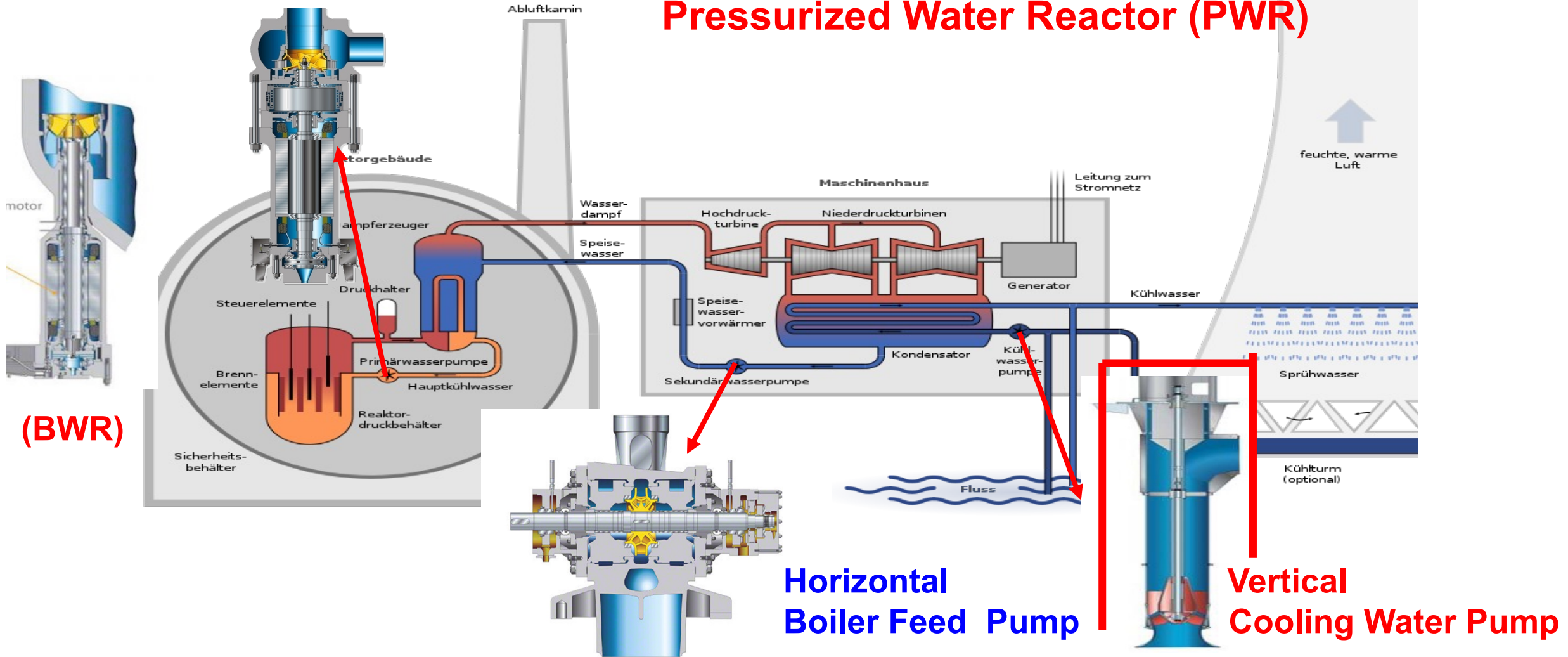
- **Different Vertical and Horizontal Pumps in Power Plants**
- **A typical Vertical Pump System for a Nuclear Power Plant**
- **Vibration Phenomena in Pump Systems**
- **Modeling of Pump Systems to predict Vibration Phenomena**
- **Monitoring of Pump Systems for Vibration Control**
- **Evaluation of Fluid Forces in Pump Systems**
- **Vibrations of a Horizontal Boiler Feed Pump due to Fluid Forces**
- **Vibrations of Vertical Pumps due to Unbalance and Instability**

Vibrations of Vertical Pumps due to Unbalance and Instability

Vertical Cooling Water Pump

Vertical Reactor Coolant Pumps (PWR)

Nuclear Power Plant Pressurized Water Reactor (PWR)

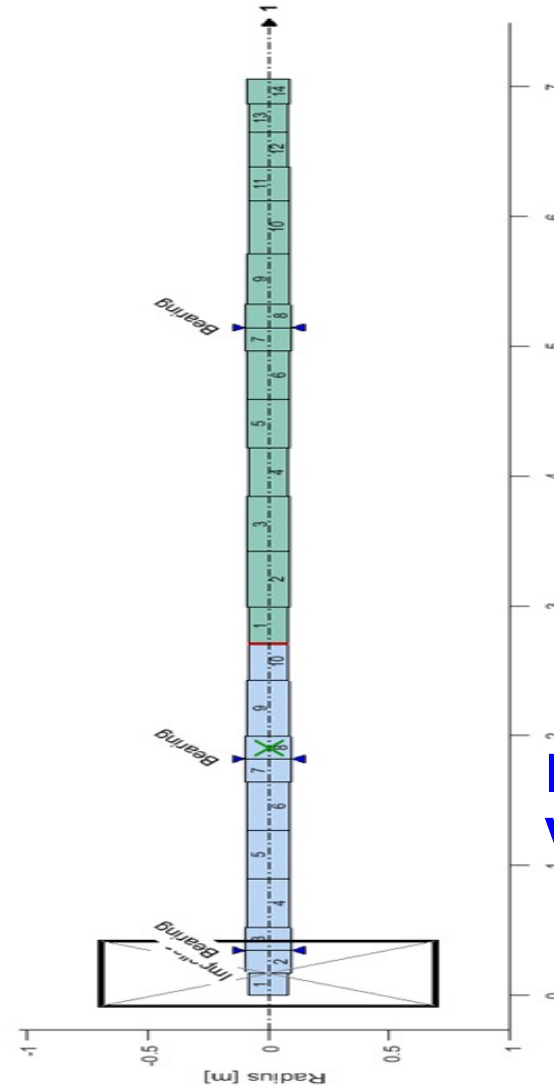


Vibrations of Vertical Pumps due to Unbalance and Instability

Vertical Cooling Water Pump



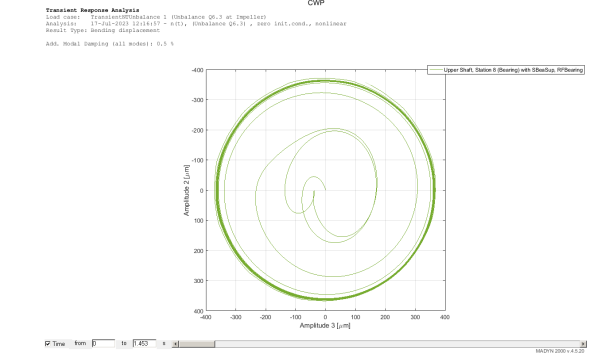
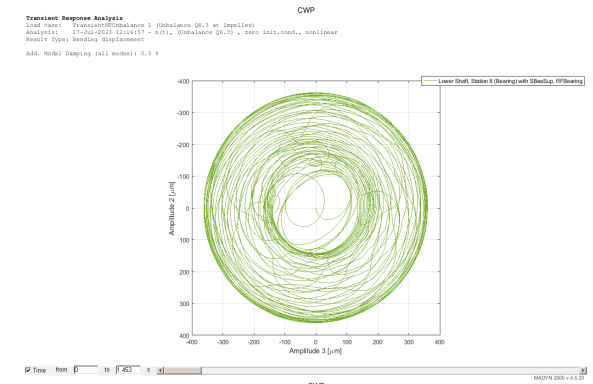
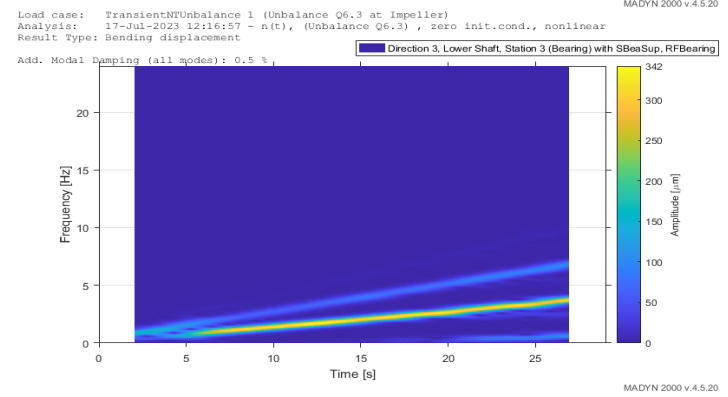
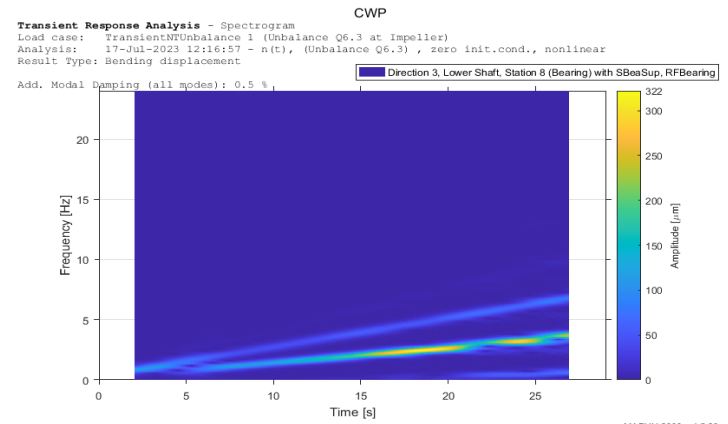
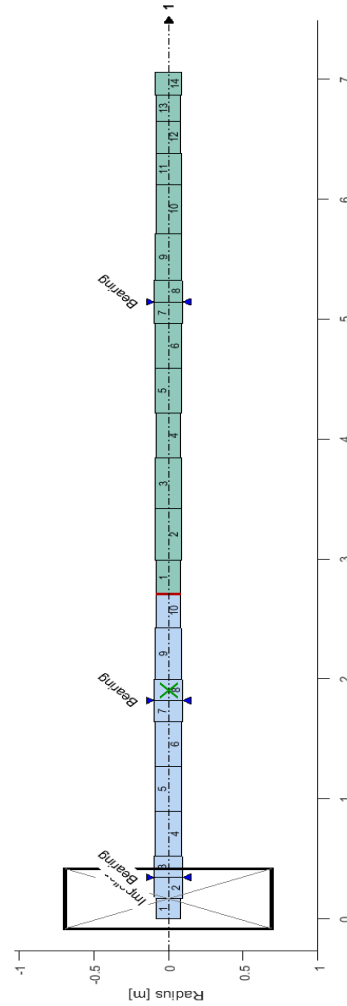
Real System of Vertical Pump



FE-Model of Vertical Pump

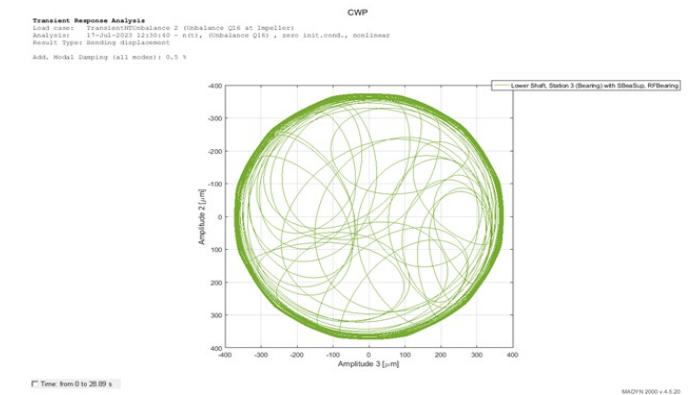
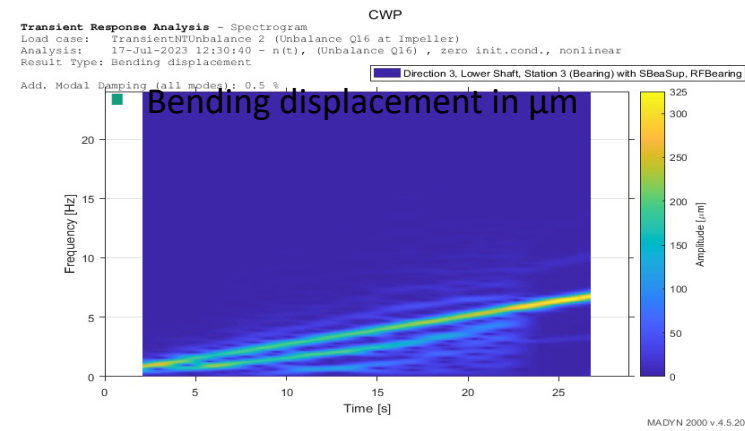
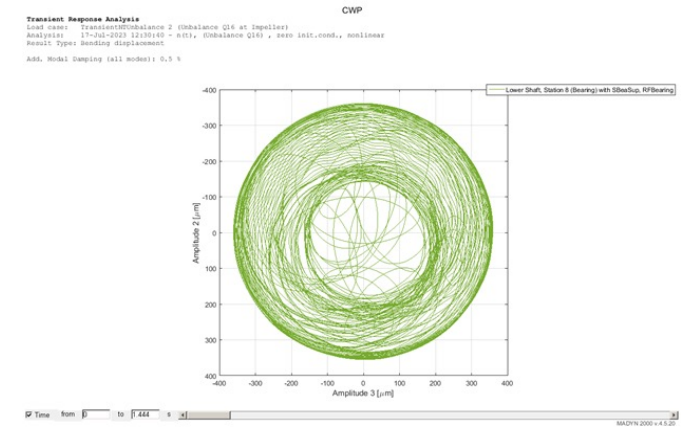
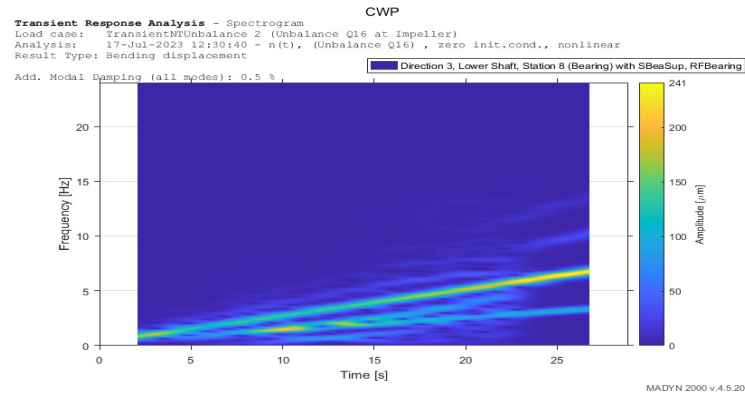
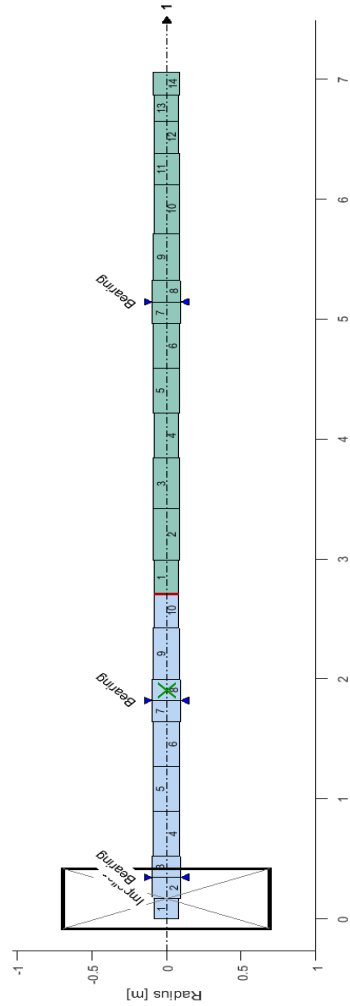
Nonlinear calculations for unbalance vibrations

Nonlinear fluid bearings, Low Unbalance, with dominant Half Frequency (Instability)



Nonlinear calculations for unbalance vibrations

Nonlinear fluid bearings , High Unbalance with dominant rotational frequency



Vorlesungen Mechatronik im Wintersemester

Vibrations in Nuclear Applications

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Pump Vibration Problems in Power Plants

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