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DARMSTADI

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Sub Synchronous Resonance (SSR) –

A Serious Electromechanical Interaction in Turbogenerators

- > Definition of Sub Synchronous Resonance (SSR)
- > Torsional Vibrations of a Turbogenerator due to Air Gap Torques
- > A simple Electrical Model with Series Compensation
- Electrical Natural Frequency and Impedance Function
- Mechanical Model for Torsional Vibrations of a Turbogenerator
- > Torsional Natural Frequencies and Mode Shapes
- Sub Synchronous Resonance in the Turbogenerator OL3

Definition of Sub Syncronous Resonance (SSR)

Turbogenerator System with Mechanical Components



Turbogenerator System with Mechanical Components

Definition of Sub Syncronous Resonance (SSR) Turbogenerator System (Mech. + Electr.) and the Electrical Grid



The Turbogenerator System with Mechanical and Electrical Components and the Electrical Grid System

Definition of Sub Syncronous Resonance (SSR)

Block-Diagram: Turbogenerator System (Mech. + Electr.) and Electrical Grid



Definition of Sub Syncronous Resonance (SSR) Model of the Turbogenerator System and the Electrical Grid





Park`sches Ersatzschaltbild



d -Achse

q - Achse

Feder-Masse-Modell



Model for the Electrical Components of Turbogenerator

Model for the Mechanical Components of Turbogenerator Sub Synchronous Resonances are oscillations in the electrical and mechanical systems, which can occur when turbine generator units feed into a network, where long lines are compensated by series capacitors.

Triggered by a fault or by switching operations in the electrical system, which represents an electrical resonant circuit, an exchange of energy between the mechanical shaft and the inductive and capacitive elements of the electrical circuit will occur.

The resulting currents generate **low frequency electrical torques** in the generator **air gap**. If the frequencies of these torques are in the vicinity of one of the lowest torsional natural frequencies, the shaft assembly will be excited to **strong resonant torsional vibrations (SSR)**.

Definition of Sub Synchronous Resonance (SSR)

Energy Exchange between the Mechanical and the Electrical System



In order to predict **Sub Synchronous Resonances** it is necessary to model the system with the greatest possible accuracy, both for the **entire network** with series and parallel capacitances as well as for the **electrical part** of the **generator** and the **mecanical shaft assembly**.

The "electro-mechanical damping" is generally low or even negative. In case of a negative damping the torsional vibrations will increase (instability!), which may lead to impermissibly high stresses and even to damages.

Definition of Sub Synchronous Resonance (SSR)

Damages due to Energy Exchange between Mechanical and Electrical System



Definition of Sub Synchronous Resonance (SSR)

IEEE (Inst. of Electrical & Electronical Engineers): Terms and Definition for SSR

Sub-synchronous resonance is an electric power system condition where the electric network exchanges energy with a turbine generator at one or more of the natural frequencies of the combined system below the synchronous frequency of the system.

(IEEE SSR Working Group, "Proposed Terms and Definitions for Subsynchronous Resonance," IEEE Symposium on Countermeasures for Subsynchronous Resonance, IEEE Pub. 81TH0086-9-PWR, 1981,p 92-97.)



Natural frequencies below the synchronous frequency

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Torsional Vibrations of a Turbogenerator due to Air Gap Torques Generator Cross Section with Rotor and Stator



Torsional Vibrations of a Turbogenerator Shaft Train can be excited by Air Gap Torques, generated due to Electro-Mechanical Interaction

Torsional Vibrations of a Turbogenerator due to Air Gap Torques Air Gap Torque due to Electro-Mechanical Interaction



$$M_{eL} = \frac{d}{d\varphi} \sum_{j=1}^{n} \sum_{k=1}^{m} L_{j,k}^{S,L}(\varphi) \cdot i_{j}^{S}(t) \cdot i_{k}^{L}(t)$$

Kulig, S.: "Simulation Models for Calculating The Tosional Vibrations ..." Springer 1981

Due to **electrical disturbances** or **switcing operations** in the generator-grid system transient **Air gap torques** M_{eL} will be generated, which excite the shaft train to **Torsional vibrations**.

The time dependent Air gap torque M_{eL} depends on electrical quantities - currents in the rotor- and stator-windings and the coupling Inductances - and on mechanical quantities.

Torsional Vibrations of a Turbogenerator due to Air Gap Torques Air Gap Torque due to Electro-Mechanical Interaction



Electro-Mechanical Interaction in the Air Gap.

Torsional Vibratios of a Turbogenerator due to Air Gap Torques Air Gap Torque due to Electro-Mechanical Interaction



Torsional Vibrations of a Turbogenerator due to Air Gap Torques Air Gap Torque due to Electro-Mechanical Interaction



Torsional Vibrations of a Turbogenerator due to Air gap Torques Frequency content in the Air Gap Torque in an SSR event

For the further discussion we define the following **frequencies**:

- The grid synchronous frequency : $f_s = \omega_s / 2 \pi = 50$ Hz
- The **electrical natural frequencies** of the electrical system (generator and grid). i = 1, 2,..I : $f_E^i = \omega_E^i/2\pi$ Hz
- The mechanical torsional natural frequencies of the Turbogenerator shaft train. j = 1,2,..J : $f_M{}^j = \omega_M{}^j/2\pi$ Hz

Torsional Vibrations of a Turbogenerator due to Air gap Torques Frequency content in the Air Gap Torque in an SSR event

After an occurrence of a fault in the electrical system oscillating currents with electrical natural frequencies f_E^i are produced in the power system. Due to these additional electrical resonant currents the Air Gap Torque consists now of the frequencies:

- the rated **grid synchronous frequency** $f_s = 50 \text{ Hz}$ and
- the **electrical natural frequencies** f_E^i sub sychronous

Example: In case of one dominant electrical Natural frequency $f_{E^{i}}$ the frequency content of the **Air Gap Torque** will be equal to the **difference**: $f_{AGT} = (f_{S} - f_{E^{i}})$

Torsional Vibrations of a Turbogenerator due to Air gap Torques Conditions for **Sub Synchronous Resonance** (**SSR**)

If one of the frequencies ($f_s - f_{E^i}$) is in the vicinity of one of the lowest **mechanical torsional natural frequencies** f_{M^j} , the shaft assembly will be excited to strong resonant torsional vibrations.

The conditions for **Sub Synchronous Resonance** are:

$$f_M{}^j$$
 = ($f_S - f_E{}^i$) = $f_{AGT} = f_{SSR}{}^i$

- f_M^j Torsional natural frequency of the Shaft
- f_Eⁱ Electrical natural frequency
- f_S Synchronous frequency of the Grid

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A simple Electical Model with Series Compensation Complement of the electrical natural frequencies

- In order to evaluate the SSR-Sensitivity of a Turbogenerator-System with its mechanical and electrical components and the Electrical Grid, the conditions for a Sub Synchronous Resonance have to be studied.
- As shown before, the probability for an SSR event is high, if one of the torsional natural frequencies f_M^j is close to the complement of the electical natural frequencies: (f_S f_Eⁱ).
- The key for the evaluation of an SSR event is therefore the knowledge of the electrical natural frequencies f_Eⁱ and the natural frequencies f_M^j
- In the following explanation we start with a very simple Model of an Electrical System (Generator plus Grid) with series compensation.

A simple Electrical Model with Series Compensation Transmission Lines with Series Compensation

• Transmission Lines are mainly characterized by series Inductive Reactance $X_L = L \omega_s$ and by a Resistance R



- The X_L value can limit the maximum allowable transfer, especially across long lines
- Additional in series-connected capacitors $X_C = 1/(C \omega_S)$ reduce the total reactance and increase the maximum transfer across the line.



A simple Electrical Model with Series Compensation

Simple Electrical Circuit Model (Grid plus Generator)



U(t) Voltage, I(t) Current, R Resistance, L Inductance, C Capacity

This very **simple Electric Circuit Model** shows the basic components of an electric circuit. A real Electrical Model contains much more electrical components of the Grid and in addition also components of the electrical part of the Generator.

However, with this simple model we can explain in an easy way the basic relations for an **Sub Synchronous Resonance (SSR)** event and how the electrical natural frequencies and the Impedance function can be determined and used for an evaluation of SSR.

Sub-Synchronous Resonance in Turbogenerators –

A Serious Torsional Vibration Problem

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Electrical Natural Frequency and Impedance Function

Diff. Equations and Eigenvalues of the Electrical Model with Resistance R



Diff. Equation for the **Electrical Circuit**:

$$R I + L dI/dt + 1/C \int I dt = U(t)$$

U(t) Voltage, I(t) Current, R Resistance, L Inductance, C Capacity



They express: Electrical Damping Electrical Natural Circular frequency $\omega_E = 2 \pi f_E$

Electrical Natural Frequency and Impedance Function

Diff. Equations and Eigenvalues of the Electrical Model without Resistance R



Diff. Equation for the **Electrical Circuit**:

$$\lambda_{1,2} = +/- j \lambda_{imag} = +/- j \sqrt{(1/CL)} = +/- j \omega_E$$

Electrical Natural Circular Frequency without Resistance: $\omega_E = \sqrt{1/CL}$

If we introduce the **Reactances** $X_L = L \omega_S$ and $X_C = 1/(C \omega_S)$ we obtain

$$\omega_{\rm E} = \omega_{\rm S} \sqrt{(X_{\rm C} / X_{\rm L})}$$

 ω_{s} Synchronous frequency of the Grid

Electrical Natural Frequency and Impedance Function Electrical Natural Frequency of the Model **without Resistance**

The Electrical Natural Circular Frequency ω_E of the circuit can be influenced by the Inductive and Capacitive Reactances X_L , X_C

$$\omega_{\rm E} = \omega_{\rm S} \sqrt{(1 X_{\rm C} / X_{\rm L})}$$

- ω_{E} Electrical natural circular frequency
- ω_s Synchronous frequency of the Grid
- $X_L\,, X_C\,\,$ Inductice and Capacitive Reactances



The Impedance Function Imp is defined as the ratio Voltage/Current for the case of a Harmonic Excitation I(t) with a circular frequency ω

In complex notation $\underline{I}(t) = \hat{\underline{I}} e^{j\omega t}$, $\underline{U}(t) = \hat{\underline{U}} e^{j\omega t}$ (j = imaginary unit) we obtain the Impedance Function Imp(j ω) for the simple Electrical Model

 $Imp (j\omega) = \widehat{U} / \widehat{I} = \{R + j\omega L + 1 / (j\omega C\} = Re (Imp) + jIm (Imp) / (j\omega) = \widehat{U} / \widehat{I} = R + j(\omega L - 1 / \omega C) = R + j(X_L - X_C)$

The following information can be obtained from the Impedance Function

- Re (Imp (jω)) : R expresses the Resistance (damping) of the simple Electrical circuit. In general if Re (Imp (j ω)) is negative, the Electrical system is unstable!
- Im (Imp (j ω)) : If (X_L X_C) = 0, then $\omega^2 = 1 / (LC) = \omega_E^2$ Im (Imp (j ω) = 0 means, that the electrical grid is in a **Resonance Condition**. ω_E is the **Resonance Frequency** of the **Electrical Circuit**

Electrical Natural Frequency and Impedance Function Example of an Impedance Function Imp (j ω)

- The investigation of the Impedance Function of the Electrical System (Electrical part of the Generator and the Grid) is a suited method to predict the possible occurrence of an SSR event.
- The following diagram shows an example of an Impedance Function in Amplitude and Phase presentation. Three cases of different compensation rates X_c are shown in the frequency range from 0 to 60 Hz.
- The Electrical Resonance Frequencies for the different compensations can be determined at frequencies, where the Amplitude of the Impedance Function is Zero (26 Hz, 35 Hz and 42 Hz). If in this 60Hz (synchr. frequency) application the Mechanical Natural Frequencies are at the complement frequences 18 Hz and/or 34 Hz, the conditions of an SSR event are most likely.

Electrical Natural Frequency and Impedance Function

Amplitude and Phase of an Impedance Function for different compensations



Electrical Natural Frequency and Impedance Function Example of Impedance Functions of the Finish Grid close to OL3

- The following diagram shows calculated frequency-dependent amplitudes of four Impedance Functions for different topologies of the Finish Grid close to the OL3 Turbogenerator System. The Impedance scans present the network plus the integrated Generator as seen from the Generator terminals.
- The solid red curve presents the Impedance Function of one topology, in which an SSR event occured in reality at the OL3 Turbogenerator. The calculated Impedance Function did not reach a value of zero, however a minimum has been predicted at a frequency of 34,5 Hz.
- If the frequency at this Minimum can be interpreted as one of the electrical natural frequencies f_Eⁱ = 34,5 Hz of the Grid plus Generator, an occurence of SSR can be expected at the frequency of (f_S f_Eⁱ) = 15.5 Hz. This value fits quite well to one of the torsional natural frequencies of 14,4 Hz.

Electrical Natiural frequency and Impedance Function Impedance Function of the Finish Grid close to the OL3 Turbogenerator



Impedance from generator terminals as a function of frequency

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Mechanical Model for Torsional Vibrations of a Turbogenerator Mass and Stiffness Distribution along the Shaft Train (Finite Elements)

The Mechanical Model of a general Turbogenerator Shaft Train can be built up by means of the Finite Element Method.

Each Finite Element will be described by its **length**, the **moment of inertia** and the **torsional stiffness**.



Mechanical Model for Torsional Vibrations of a Turbogenerator FE-Model and Equations of Motion for Torsional Vibrations



The linear Equations of the Torsional Motion are built up of mass, damping and stiffness matrices of the shaft train and the torque vector $M_{eL}(t)$ due to the Electro-Mechanical Interaction in the Air Gap. q (t) is the vector of the angular displacements.

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Torsional Natural Frequencies and Mode Shapes

Assessment of Torsional Vibrations in the Design – Eigenvalue Analysis



An Eigenvalue Analysis leads to the **Torsional Natural Frequencies** $\omega_M{}^j$ and to the corresponding **Mode Shapes** $\phi_M{}^j$. The **damping** in the shaft train is **low**. Therefore the natural frequencies are not influenced by the damping: **D** ~ 0.

$$(\mathbf{K} - \boldsymbol{\omega}^2 \cdot \mathbf{M}) \cdot \boldsymbol{\varphi} = \mathbf{0}$$

Torsional Natural frequencies $\omega_M{}^j$ **Torsional Mode shapes** $\phi_M{}^j$

Modal Damping in % with and without Electrical Load Estimation of Mechanical and Electrical Damping at OL3 Turbogenerator

		Without electric With electric	
		load, after	load, (~950
		disconnection	MW)
		Modal	Modal
	Freq.	damping ratio	damping ratio
A damata			
Mode	(Hz)	ζ (%)	ζ (%)
Mode 1	(Hz) 5.8	ζ (%) 0.008	ζ (%) 0.22
Mode 1 2	(Hz) 5.8 10.6	ζ (%) 0.008 0.005	ζ (%) 0.22 0.07

Modal Damping in % with and without Electrical Load

Torsional Natural Frequencies and Mode Shapes

Example: Lowest Torsional Natural Frequencies and Mode Shapes of OL3

- The four lowest Torsional Natural Frequencies $f_M{}^j = \omega_M{}^j/2 \pi$ Hz of the OL3 Turbogenerator Shaft Train are presented in the next diagram together with the corresponding Mode Shapes $\phi_M{}^j$. They are in the range between 5,9 Hz to 24,0 Hz and are relevant for a Sub Synchronous Resonance (SSR) event.
- The first three Modes can be well excited by an Air Gap Torque, due to the fact, that these Modes have dominant angular displacements in the Generator part. This is particularly the case for the 3rd mode at 14,6 Hz. Therefore this frequency is very sensitive regarding SSR.
- The Blade-Rotor-Coupling is not relevant for these lower Modes and can be neglected. The blades are only considered by their moments of inertia.

Torsional Natural Frequencies and Mode Shapes

Example: Lowest Torsional Natural Frequencies and Mode Shapes of OL3



Torsional Natural Frequencies: $f_M{}^j = \omega_M{}^j / 2 \pi$ Hz (j = 1, 2...4)

Mode Shapes of the **Shaft Train**: $\phi_{M^{j}}$

Torsional Natural Frequencies and Mode Shapes Example: Measurement of Torsional Natural Frequencies of OL3

The before mentioned four Torsional Natural Frequencies f_M^j [Hz] have also been measured during operation of the OL3
Turbogenerator Shaft Train. They have been detected besides other frequencies in the lower range of the Frequency Spectrum (next diagram). As can be seen the measured frequencies fit quite well to the calculated values:

	Measured Torsional Frequency	Calculated Torsional Frequency
1.	5,67 Hz	5,9 Hz
2.	10,63 Hz	10,9 Hz
3.	14,37 Hz	14,6 Hz
4.	23,23 Hz	24,0 Hz

Torsional Natural Frequencies and Mode Shapes

Example: Measurement of Torsional Natural Frequencies of OL3



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Repetition:

If one of the frequencies ($f_{s} - f_{E}^{i}$) is in the vicinity of one of the lowest **mechanical torsional natural frequencies** f_{M}^{j} , then the shaft assembly will be excited to **strong resonant torsional vibrations**.

The conditions for **Sub Synchronous Resonance** are therefore:

$$f_M{}^j$$
 = ($f_S - f_E{}^i$) = $f_{SSR}{}^i$

- f_M^j Torsional natural frequency of the Shaft
- f_Eⁱ Electrical natural frequency of the Grid
- f_S Synchronous frequency of the Grid (50 Hz)

Sub Synchronous Resonance in the Turbogenerator OL3 Monitoring of the SSR event on 5.1.23 by SSR sensors (loc. 3, 5, 8)



Maximum stress at loc.8

Sub Synchronous Resonance in The Turbogenerator OL3 Monitoring of the OL3-SSR event 1 on 5.1.23 by SSR1 sensor at loc.8



frequency

Sub Synchronous Resonance in the Turbogenerator OL3 Monitoring of the OL3-SSR event 2 on 5.1.23 by SSR1 sensor at loc.8



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